

# Dark matter direct detection at one loop

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Michael A. Schmidt

12 December 2017

CosPA 2017

based on

C. Hagedorn, J. Herrero-García, E. Molinaro, MS [1712.xxxxx]

J. Herrero-García, E. Molinaro, MS [1712.xxxxx]



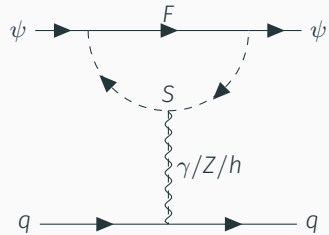
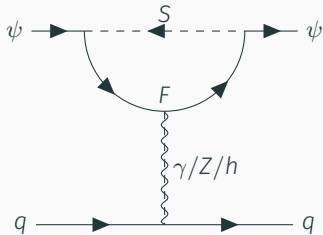
THE UNIVERSITY OF  
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**CoEPP**  
ARC Centre of Excellence for  
Particle Physics at the Terascale

# Motivation

- No clear evidence for DM in direct/indirect detection or at LHC
- Only hints from DAM.\*
- Option: DM is not directly coupled to quarks
- Examples: fermionic singlet DM  $\psi$  such as bino, fermionic DM in scotogenic model, or models explaining the DAMPE result
- Direct detection occurs at one loop
- Next generation (liquid noble gas) experiments could probe it



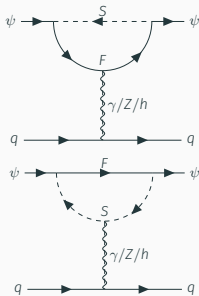
# Simplified fermionic DM model

Dark sector	Field	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	$U(1)_{dm}$
Dark matter	$\psi$	1	1	0	1
Dark scalar	$S$	1	$d_F$	$Y_F$	$q_s$
Dark fermion	$F$	1	$d_F$	$Y_F$	$q_s + 1$

$$\mathcal{L}_\psi = i\bar{\psi}\not{\partial}\psi - m_\psi\bar{\psi}\psi + i\bar{F}\not{\partial}F - m_F\bar{F}F + (D_\mu S)^\dagger D^\mu S$$

$$- \left( y_1 \bar{F}_R S \psi_L + y_2 \bar{F}_L S \psi_R + \text{H.c.} \right) - \lambda_{HS} v h S^\dagger S + \dots$$

- Higgs portal coupling may arise in different ways
- Easy to generalise to larger dark symmetry groups



# Simplified fermionic DM model

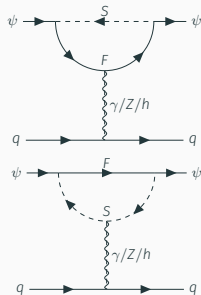
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## SM fields in loop

1.  $F \rightarrow L_L/e_R$ :  $\psi$  or  $S$  have  $L = 1$  LFV, EDM/AMMs, LNV
2.  $F \rightarrow \nu_R$ :  $\nu_R$  and  $\psi$  or  $S$  have  $L = 1$  Gonzalez-Macias, Escudero, ...
3.  $S \rightarrow H$ : mixing  $\psi - F_0$ , thus tree-level  $H/Z$  exchange



# (Relevant) effective interactions for direct detection

## Dirac DM

- Electric and magnetic dipoles:  $\mathcal{L} = \mu_\psi \mathcal{O}_{\text{mag}} + d_\psi \mathcal{O}_{\text{edm}}$  [long-range]

$$\mathcal{O}_{\text{mag}} = \frac{e}{8\pi^2} (\bar{\psi} \sigma^{\mu\nu} \psi) F_{\mu\nu}, \quad \mathcal{O}_{\text{edm}} = \frac{e}{8\pi^2} (\bar{\psi} \sigma^{\mu\nu} i\gamma_5 \psi) F_{\mu\nu},$$

- Vector interactions induced by  $Z/\gamma$ -penguins [anapole  $(\bar{\psi} \gamma^\mu \psi)(\partial^\nu F_{\mu\nu}) \equiv \mathcal{O}_{\text{SI}}^V$  by EOM]

$$\mathcal{O}_{\text{SI}}^V = (\bar{\psi} \gamma^\mu \psi)(\bar{q} \gamma_\mu q) \quad \mathcal{O}_{\text{SD}}^{AV} = (\bar{\psi} \gamma^\mu \gamma_5 \psi)(\bar{q} \gamma_\mu \gamma_5 q),$$

- Scalar interactions [and gluon interaction induced by heavy quarks]

$$\mathcal{O}_{\text{SI}}^S = m_q (\bar{\psi} \psi)(\bar{q} q) \quad \mathcal{O}_{\text{SI}}^G = \frac{\alpha_s}{8\pi} (\bar{\psi} \psi) G^{a\mu\nu} G_{\mu\nu}^a$$

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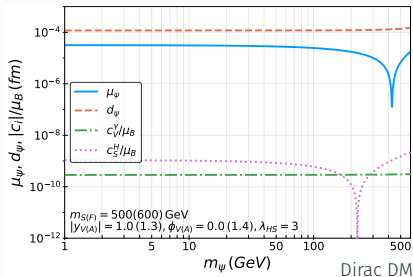
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## Majorana DM

- no dipole and vector interactions
- P-violating vector interaction [momentum suppressed]

$$\mathcal{O}_{\text{SI}}^{\text{AV}} = (\bar{\psi} \gamma^\mu \gamma_5 \psi)(\bar{q} \gamma_\mu q)$$

# Dominant interactions: electric/magnetic dipole moments



For Dirac DM  $\psi$  [ $m_\psi \ll m_F < m_S$ ]

$$\mu_\psi \approx -\frac{Q_F}{4m_S} \left( |y_V|^2 - |y_A|^2 \right) x_F \frac{1 - x_F^2 + 2 \ln x_F}{(1 - x_F^2)^2}$$

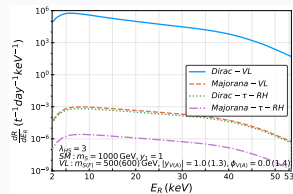
$$d_\psi \approx -\frac{Q_F}{2m_S} \text{Im}[y_V^* y_A] x_F \frac{1 - x_F^2 + 2 \ln x_F}{(1 - x_F^2)^2}$$

where

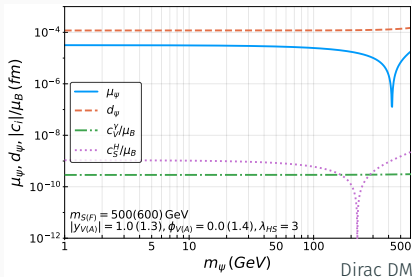
$$x_F \equiv \frac{m_F}{m_S} \quad \text{and} \quad y_{V,A} = \frac{y_2 \pm y_1}{2}$$

## Dominant contribution:

- Dirac DM: magnetic and electric dipole moments
- Majorana DM: Higgs, but also photon penguin.



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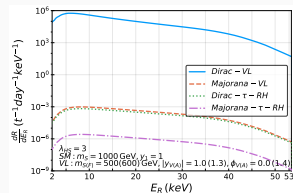
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All contributions have to be considered simultaneously

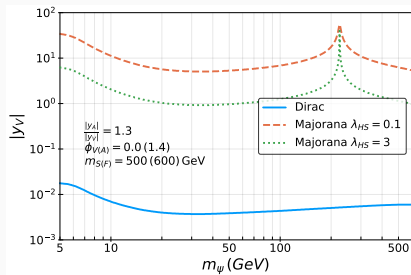
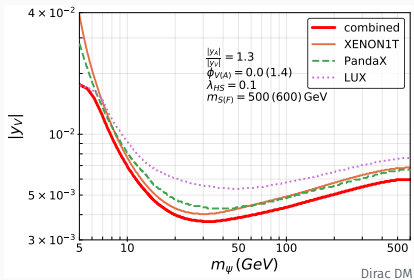


- Analytical expressions valid for general models provided in paper and compared to existing results [Berlin, Chang, Agrawal, Kumar, Schmidt, Kopp, Ibarra...](#)
- Implemented with [DirectDM](#)<sup>1708.02678</sup> and [LikeDM](#)<sup>1708.04630</sup>



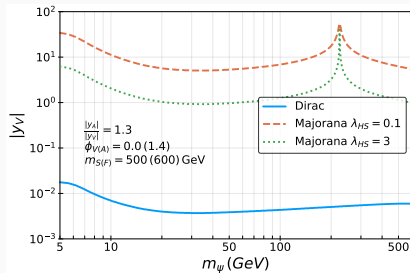
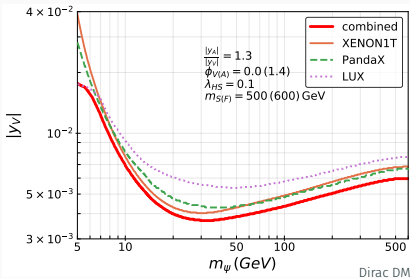
# Direct detection limits

## Vector-like fermions

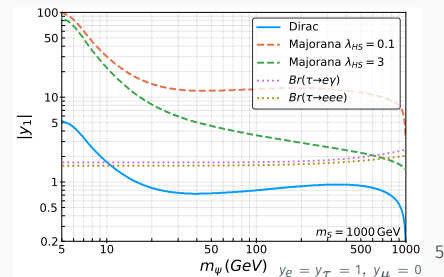
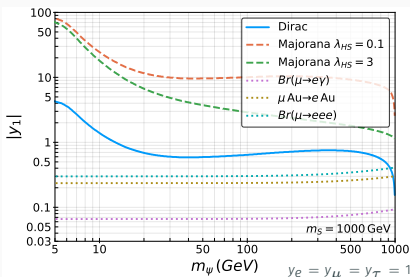


# Direct detection limits

## Vector-like fermions



## Right-handed charged leptons



Connection to neutrino masses:  
scotogenic model with Dirac fermion

# Scotogenic model with Dirac DM

Simple example of loopy DD with radiative  $\nu$  masses:

Dirac DM  $\psi$ ,  $F \equiv L_L$ ,  $S = \Phi, \Phi'$ . Dark global (anomaly-free)  $U(1)_{\text{DM}}$

Field	$SU(3)_C$	$SU(2)_L$	$U(1)_Y$	$U(1)_{\text{DM}}$
$\Phi$	1	2	1/2	1
$\Phi'$	1	2	-1/2	1
$\psi$	1	1	0	1

Just one fermionic singlet  $\psi$  needed.  $\mathbf{y}_{\Phi^{(\prime)}}$  are 3-component vectors

$$\mathcal{L}_\psi \supset i \bar{\psi} \not{\partial} \psi - m_\psi \bar{\psi} \psi - \left( y_\Phi^\alpha \bar{\psi} \tilde{\Phi}^\dagger L_L^\alpha + (y_{\Phi'}^\alpha)^* \bar{\psi} \tilde{\Phi}'^\dagger \tilde{L}_L^\alpha + \text{H.c.} \right).$$

Two neutral scalars  $\eta_0^{(\prime)}$  (mixing angle  $\theta$ ),  
two charged scalars  $\eta^{(\prime)\pm}$  (no mixing)

$$V \supset \lambda_{H\Phi\Phi'} \left[ (H^\dagger \tilde{\Phi}') (H^\dagger \Phi) + \text{H.c.} \right] \quad \longrightarrow \quad \sin 2\theta \propto \lambda_{H\Phi\Phi'}.$$

# Different classifications

Introduction

Discussion

Survey of models



Y. Cai, J. Herrero-Garcia, MS, A. Vicente, R. Volkas [1706.08524]

REVIEW  
published 04 December 2017  
doi:10.3389/fphy.2017.00083



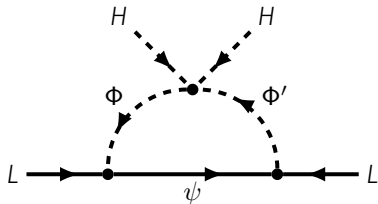
## From the Trees to the Forest: A Review of Radiative Neutrino Mass Models

Yi Cai<sup>1,2</sup>, Juan Herrero Garcia<sup>3\*</sup>, Michael A. Schmidt<sup>4\*</sup>, Avelino Vicente<sup>5</sup> and Raymond R. Volkas<sup>2</sup>

<sup>1</sup>School of Physics, Sun Yat-sen University, Guangzhou, China, <sup>2</sup>ARC Centre of Excellence for Particle Physics at the Terascale, School of Physics, The University of Melbourne, Melbourne, VIC, Australia, <sup>3</sup>ARC Centre of Excellence for Particle Physics at the Terascale, Department of Physics, The University of Adelaide, Adelaide, SA, Australia, <sup>4</sup>ARC Centre of Excellence for Particle Physics at the Terascale, Institut de Física Corpuscular (CSIC)-Universitat de València, Valencia, Spain

A plausible explanation for the lightness of neutrino masses is that neutrinos are loops, with their mass (typically Majorana) being generated from tree level, together with the suppression of the new degrees of freedom cannot be tested using different searches, making the new particle signals in lepton-flavor and neutrinos, which are not mixings. The main space from

# Majorana $\nu$ mass



$$\mathcal{M}_\nu^{\alpha\beta} = \frac{\sin 2\theta m_\psi}{32\pi^2} \left( y_\Phi^\alpha y_{\Phi'}^\beta + y_{\Phi'}^\alpha y_\Phi^\beta \right) \left[ \frac{m_{\eta_0}^2}{m_{\eta_0}^2 - m_\psi^2} \log \frac{m_{\eta_0}^2}{m_\psi^2} - (\eta_0 \leftrightarrow \eta'_0) \right]$$

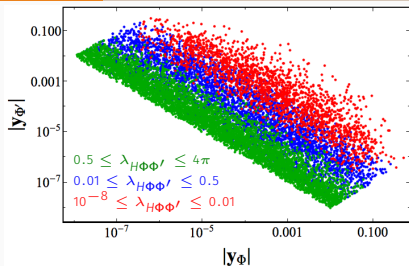
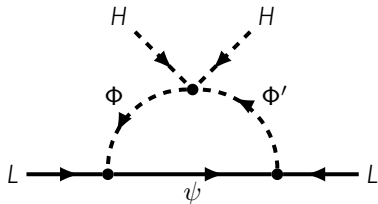
Lepton number  $L$  violated by combination of  $y_\Phi, y_{\Phi'}, \lambda_{H\Phi\Phi'} (\sin 2\theta), m_\psi, m_{\eta'_0} - m_{\eta_0}$

$\mathcal{M}_\nu$  is rank 2, so one massless  $\nu$  and two massive

$$m_\nu^\pm \propto \left( |y_\Phi| |y_{\Phi'}| \pm |y_\Phi \cdot y_{\Phi'}^\dagger| \right).$$

Yukawa vectors  $y_\Phi^{(r)}$  determined by low-energy data up to one parameter  $\zeta$  which determines relative size

# Majorana $\nu$ mass



$$\mathcal{M}_{\nu}^{\alpha\beta} = \frac{\sin 2\theta m_{\psi}}{32\pi^2} \left( y_{\Phi}^{\alpha} y_{\Phi'}^{\beta} + y_{\Phi'}^{\alpha} y_{\Phi}^{\beta} \right) \left[ \frac{m_{\eta_0}^2}{m_{\eta_0}^2 - m_{\psi}^2} \log \frac{m_{\eta_0}^2}{m_{\psi}^2} - (\eta_0 \leftrightarrow \eta'_0) \right]$$

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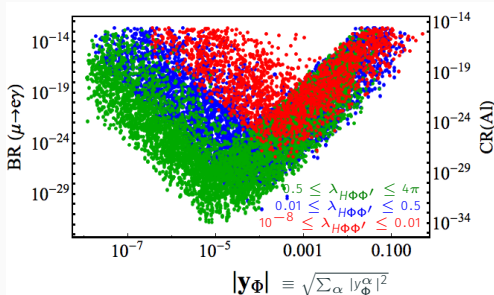
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# Lepton flavour violation: $\mu \rightarrow e \gamma$ transition

$$\text{BR}(\mu \rightarrow e \gamma) = \frac{3 \alpha_{\text{em}}}{64 \pi G_F^2} \left| \frac{y_{\Phi}^{\beta*} y_{\Phi}^{\alpha}}{m_{\eta_{\pm}}^2} f\left(\frac{m_{\psi}^2}{m_{\eta_{\pm}}^2}\right) + \frac{y_{\Phi'}^{\beta*} y_{\Phi'}^{\alpha}}{m_{\eta'_{\pm}}^2} f\left(\frac{m_{\psi}^2}{m_{\eta'_{\pm}}^2}\right) \right|^2$$

$$\text{CR(Al)} \simeq [0.0077, 0.011] \times \text{BR}(\mu \rightarrow e \gamma) \quad \text{Dipole dominance}$$

Only free parameters: masses  $m_{\psi}$ ,  $m_{\eta_{\pm}}$ , and  $\zeta$





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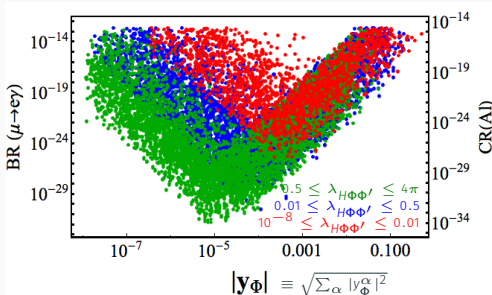
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$$\text{NO : } y_\Phi = \frac{\zeta}{\sqrt{2}} (\sqrt{m_{\text{sol}}} u_2^* \pm i \sqrt{m_{\text{atm}}} u_3^*) \quad y_{\Phi'} = \frac{1}{\zeta \sqrt{2}} (\sqrt{m_{\text{sol}}} u_2^* \mp i \sqrt{m_{\text{atm}}} u_3^*)$$

$$\text{IO : } y_\Phi = \frac{\zeta}{\sqrt{2}} (\sqrt{m_{\text{sol}}} u_1^* \pm i \sqrt{m_{\text{atm}}} u_2^*) \quad y_{\Phi'} = \frac{1}{\zeta \sqrt{2}} (\sqrt{m_{\text{sol}}} u_1^* \mp i \sqrt{m_{\text{atm}}} u_2^*)$$



with  $u_i$  being the columns of the PMNS matrix

$$\text{Using } f\left(\frac{m_{\eta^\pm}^2}{m_\psi^2}\right) \xrightarrow{m_{\eta^\pm} \rightarrow m_\psi} \frac{1}{12}$$

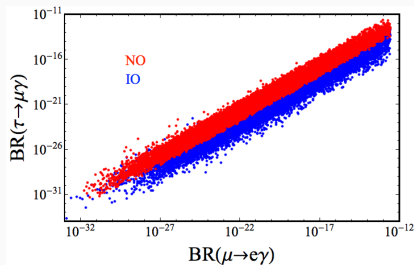
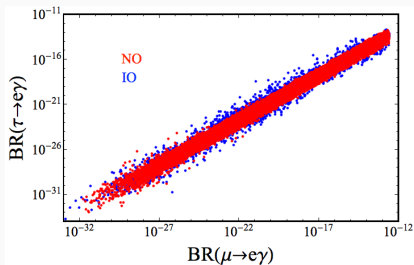
$$\text{NO : } 0.0003 \frac{100 \text{ GeV}}{m_{\eta'^\pm}} \lesssim \zeta \lesssim 4000 \frac{m_{\eta^\pm}}{100 \text{ GeV}}$$

$$\text{IO : } 0.0004 \frac{100 \text{ GeV}}{m_{\eta'^\pm}} \lesssim \zeta \lesssim 3000 \frac{m_{\eta^\pm}}{100 \text{ GeV}}$$

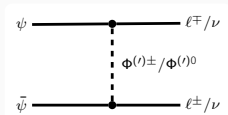
# Correlation between different LFV rates

$$\text{NO} : \frac{\text{BR}(\tau \rightarrow e \gamma)}{\text{BR}(\mu \rightarrow e \gamma)} \approx 0.2 \quad \text{and} \quad \frac{\text{BR}(\tau \rightarrow \mu \gamma)}{\text{BR}(\mu \rightarrow e \gamma)} \approx 5$$

$$\text{IO} : \frac{\text{BR}(\tau \rightarrow e \gamma)}{\text{BR}(\mu \rightarrow e \gamma)} \approx \frac{\text{BR}(\tau \rightarrow \mu \gamma)}{\text{BR}(\mu \rightarrow e \gamma)} \approx 0.2 ,$$



# DM s-wave annihilations into leptons and LFV



$$\xrightarrow{\text{ch. lep.}} \langle v\sigma_{\ell\ell} \rangle = \frac{1}{32\pi m_\psi^2} \left| y_\Phi^\alpha y_{\Phi'}^{\beta*} \frac{m_\psi^2}{m_{\eta^\pm}^2 + m_\psi^2} - y_{\Phi'}^\alpha y_\Phi^{\beta*} \frac{m_\psi^2}{m_{\eta'^\pm}^2 + m_\psi^2} \right|^2$$

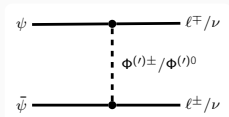
Only depends on masses and  $\zeta$  and thus strongly constrained by LFV

A conservative estimate

$$\frac{\sum_{\alpha,\beta} \langle v\sigma(\psi\bar{\psi} \rightarrow \ell_\alpha^- \ell_\beta^+, \nu_\alpha \nu_\beta) \rangle}{\langle v\sigma \rangle_{\text{th}}} \lesssim 1(0.3) \times 10^{-6} \left( \frac{3 \times 10^{-26} \text{cm}^3/\text{s}}{\langle v\sigma \rangle_{\text{th}}} \right) \left( \frac{m_\psi}{100 \text{ GeV}} \right)^2$$

for  $m_{\eta'_0} \simeq m_{\eta^\pm} \simeq m_\psi$ . Larger scalar masses lead to a further suppression. This is confirmed by numerical scan with micrOMEGAs.

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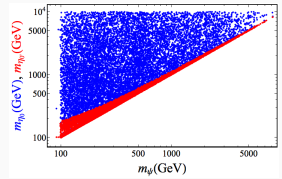
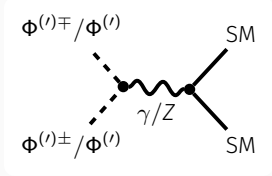
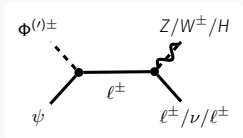
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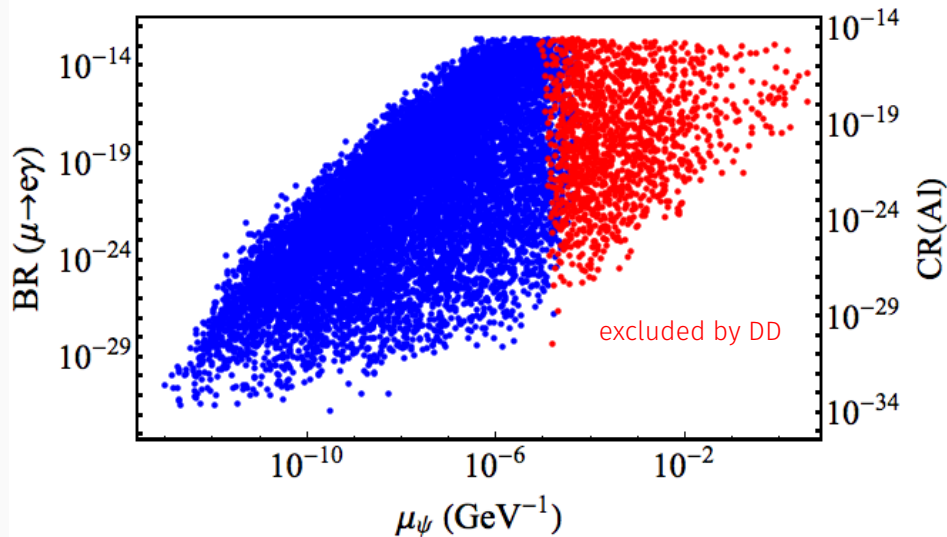
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**Annihilations into leptons too small:** need coannihilation with scalars  $\Phi^{(\prime)}$



# Complementarity of LFV and DM direct detection



## Conclusions

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DM may not couple directly to quarks

DM - nucleus scattering only at 1-loop order (or higher)

Discussion of simplified fermionic DM model

magnetic and electric dipole moment dominate

Higgs penguins are important for Majorana DM

Scotogenic model with Dirac fermion

fermionic DM requires coannihilation

interplay between LFV and direct detection

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Thank you!