

Searches for cLFV at Current and Future Colliders

Michael A. Schmidt

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UNSW
SYDNEY

Motivation

The Standard Model is very successful...

...but incomplete

In particular neutrinos are massive

Lepton flavour is not conserved

→ Flavour changing processes are a sensitive probe

- in SM + m_ν , suppressed by unitarity, $\mathcal{A} \sim G_F m_\nu^2 \simeq 10^{-26}$
- many neutrino mass models have large charged LFV due to non-unitarity or new contributions, e.g. inverse seesaw, radiative mass models
- could be completely unrelated to neutrino mass, e.g. SUSY

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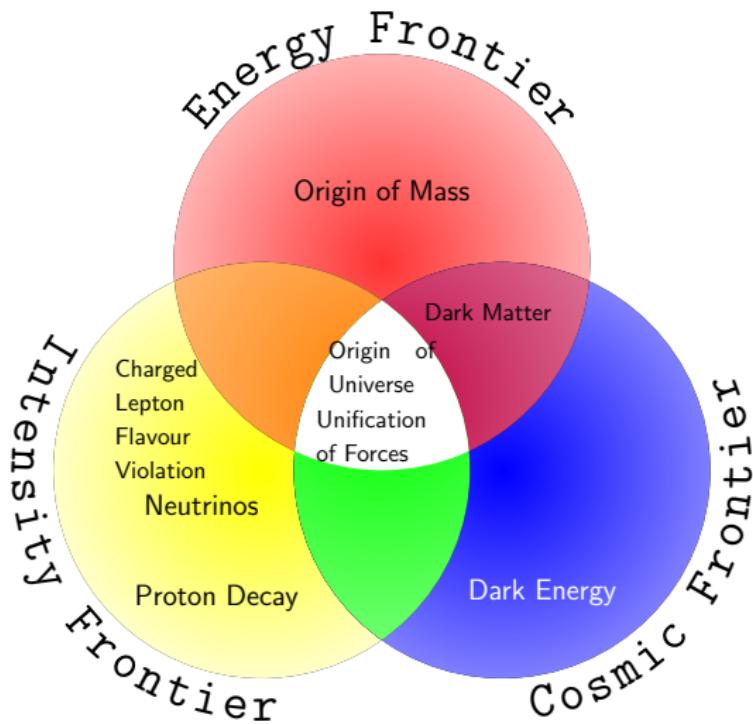
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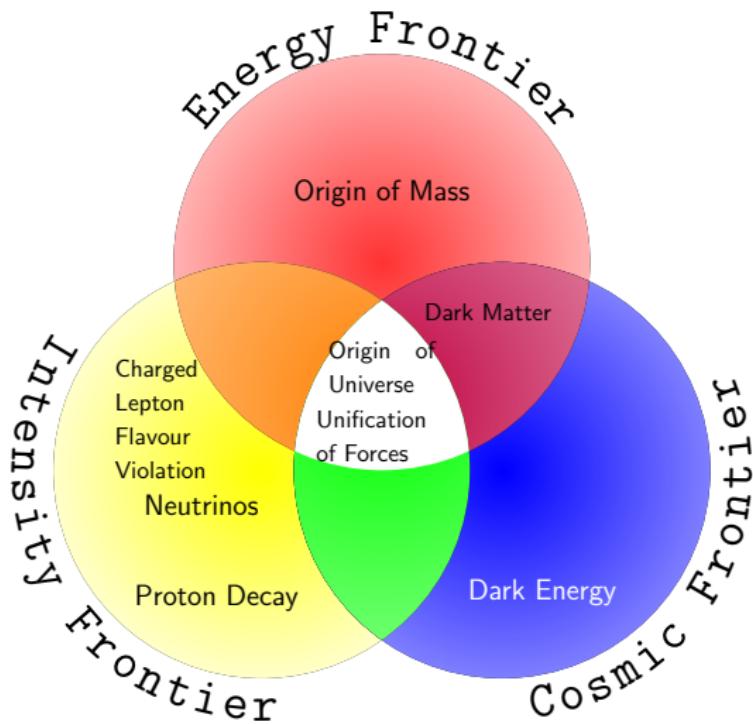
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Can high-energy colliders compete with the intensity frontier?

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Overview

Z boson decays

Higgs boson decay

Top-quark decay

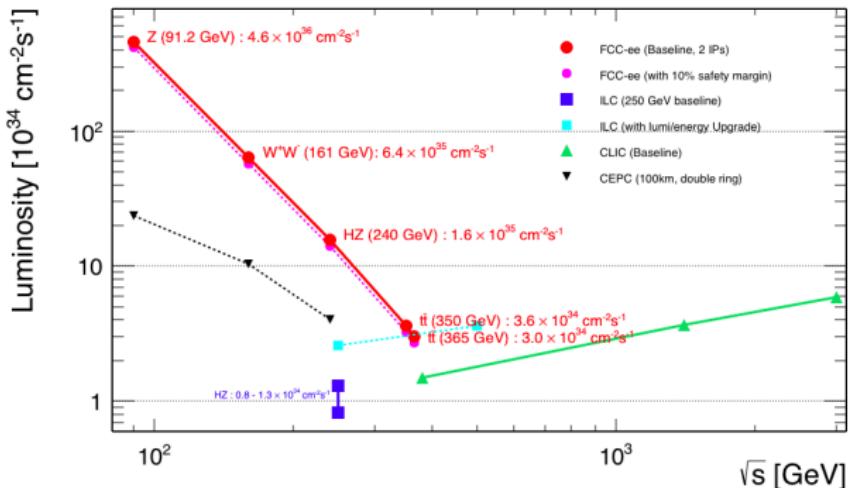
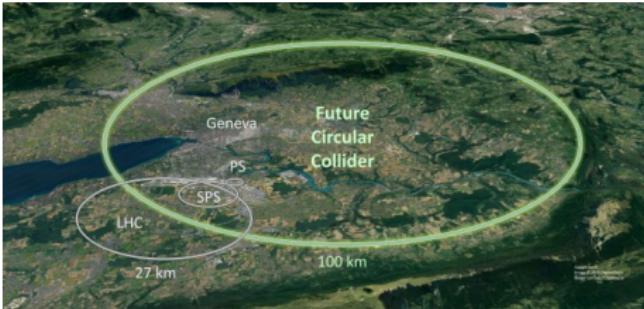
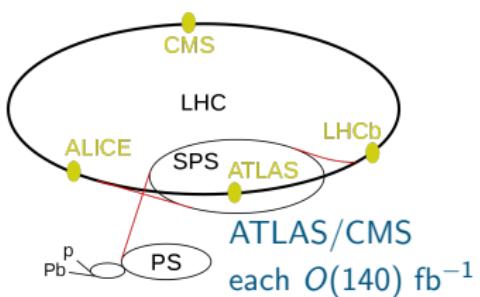
Heavy resonance decay

Scattering at the LHC

Scattering at future lepton colliders

Conclusions

Colliders



e.g. CEPC quotes

CEPC 1811.10545

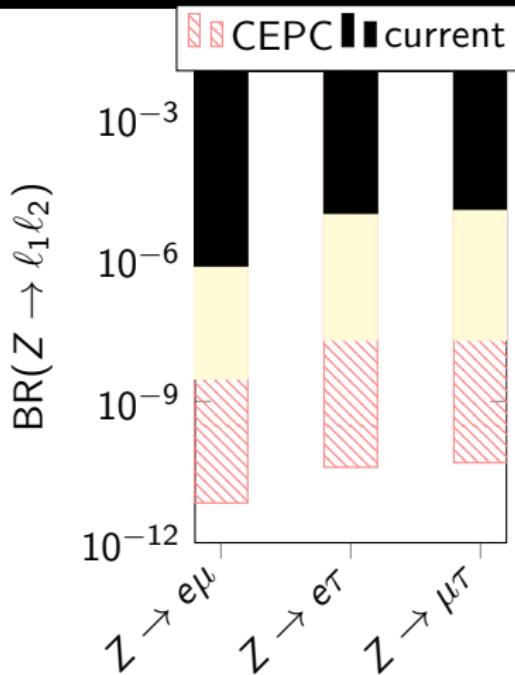
10^6 Higgs bosons

10^{12} Z bosons

LEP: $O(10^7)$ Z bosons

Z boson decays

cLFV Z boson decays



$Z \rightarrow e\mu$: ATLAS 1408.5774, CMS EXO-13-005

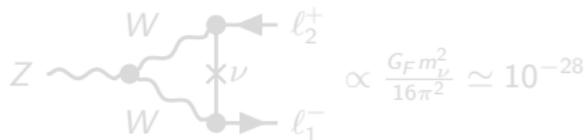
$Z \rightarrow \ell\tau$: DELPHI ($\mu\tau$), OPAL ($e\tau$)

ATLAS, 13 TeV, 36.1 fb^{-1} 1804.09568

almost same sensitivity for $\mu\tau$

See also poster on $Z \rightarrow \tau\ell$ at ATLAS by Ann-Kathrin Perrevoort

No tree-level FCNC in SM
induced at 1 loop in SM + m_ν



Observation clear sign of new physics
e.g. due to a leptoquark

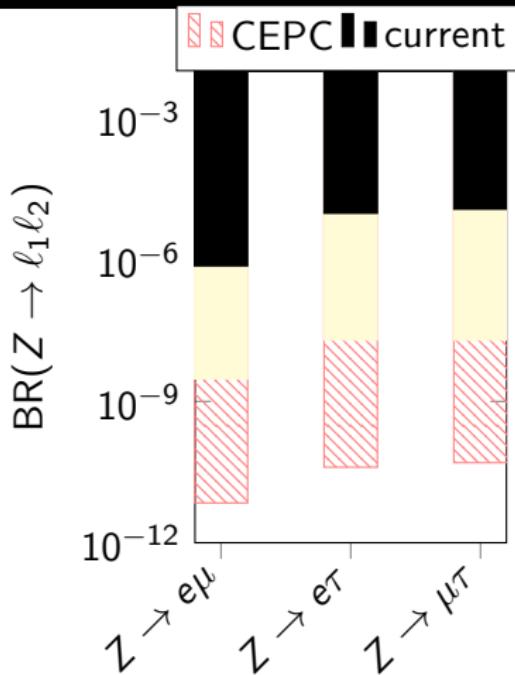


today typically less stringent as low-energy precision experiments

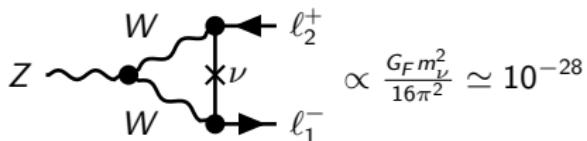
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or if there is a signal to disentangle physics

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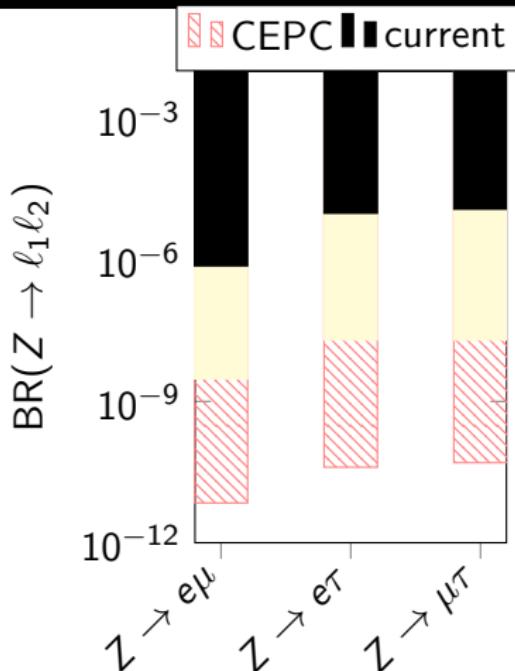
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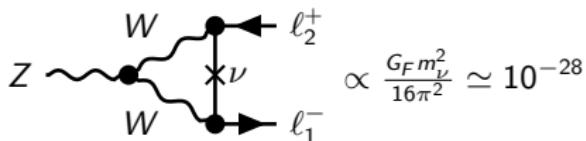
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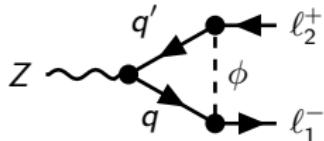
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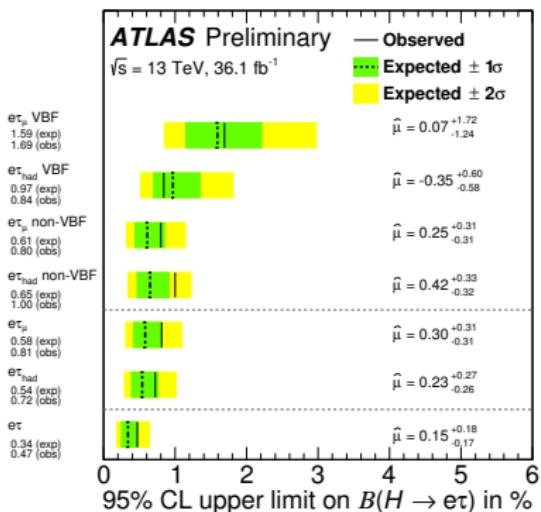
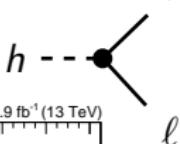
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Higgs boson decay

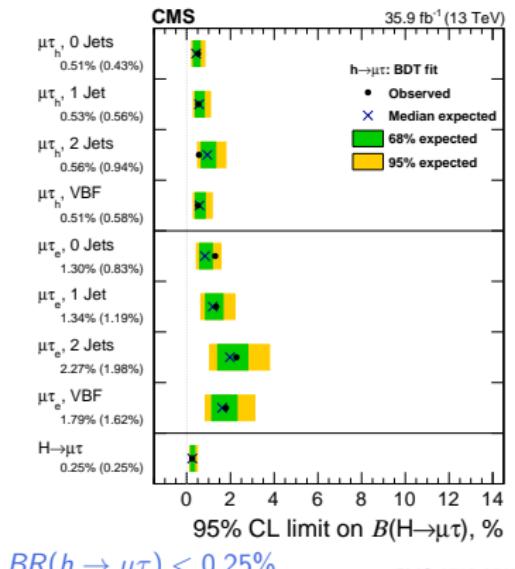
cLFV Higgs decay

Dimension-6 SMEFT operators Grzadkowski et al 1008.4884

$$\mathcal{L} = \left[Y_{ij} + \frac{c_{ij}}{\Lambda^2} (H^\dagger H) \right] \bar{L}_i P_R \ell_j H + h.c. \rightarrow \left[\frac{m_{ij}}{v} + \frac{c_{ij}}{\sqrt{2}} \frac{v^2}{\Lambda^2} \right] h \bar{\ell}_i P_R \ell_j + h.c.$$



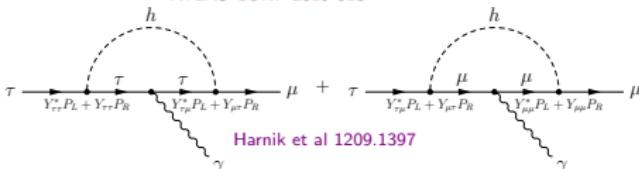
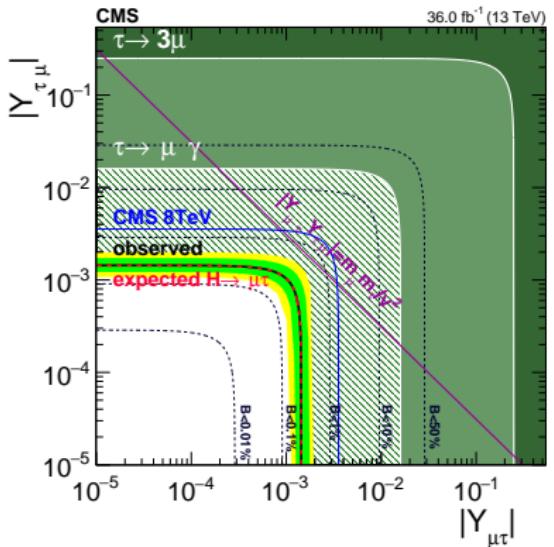
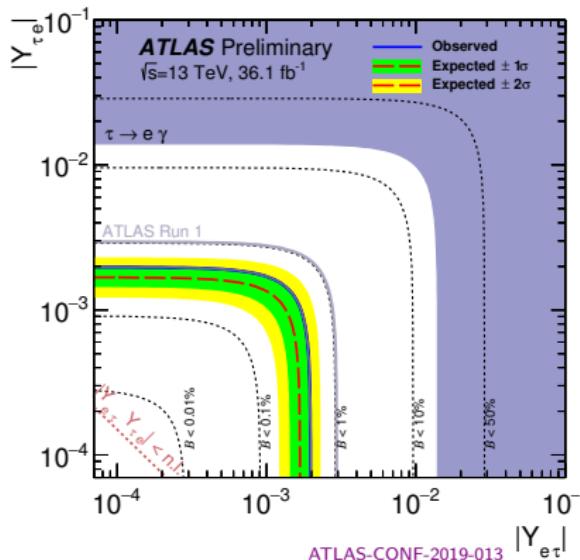
ATLAS-CONF-2019-013



CMS 1712.07173

cLFV Higgs decay cont.

$$\sqrt{|Y_{\ell\tau}|^2 + |Y_{\tau\ell}|^2} = \frac{8\pi\Gamma_H(SM)}{m_H} \frac{BR(H \rightarrow \ell\tau)}{1 - BR(H \rightarrow \ell\tau)}$$



General (type-III) 2 Higgs doublet model

EFT

$$\mathcal{L} = \left[\frac{m_i}{v} \delta_{ij} + \frac{c_{ij}}{\sqrt{2}} \frac{v^2}{\Lambda^2} \right] h \bar{\ell}_i P_R \ell_j$$

two neutral CP even Higgs

$$\Phi_i = (v_i + \phi_i)/\sqrt{2} \quad \frac{v_2}{v_1} = t_\beta$$

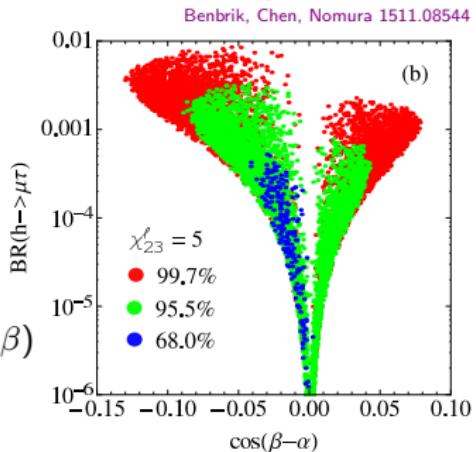
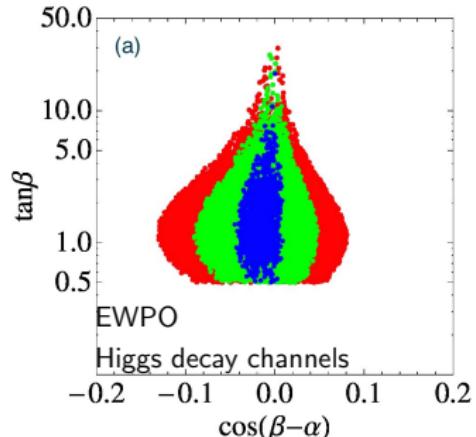
SM Higgs: $h = -s_\alpha \phi_1 + c_\alpha \phi_2$

with Yukawa couplings

$$Y_{ij} = -\frac{s_\alpha}{c_\beta} \frac{m_i}{v} \delta_{ij} + \frac{\cos(\beta - \alpha)}{c_\beta} \frac{\sqrt{m_i m_j}}{v} \chi_{ij}^\ell$$

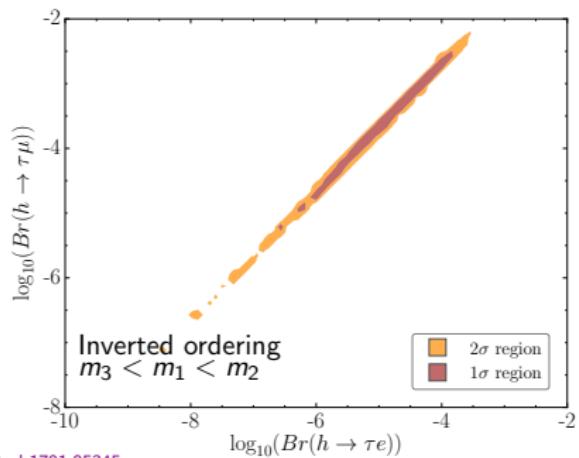
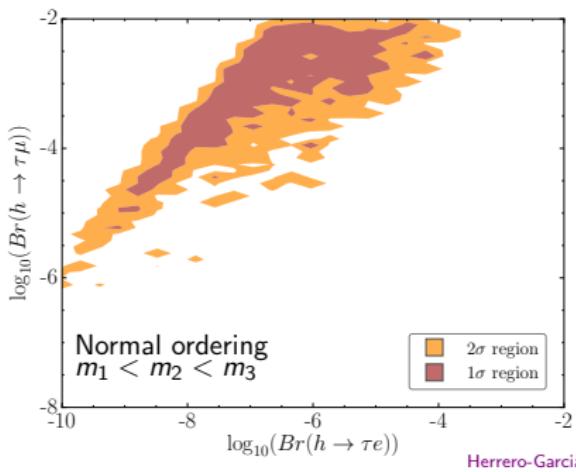
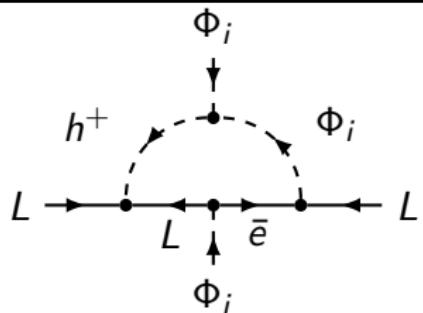
Not suppressed by $v^2/\Lambda^2 \rightarrow$ large contribution

$$BR(h \rightarrow \mu\tau) \propto (|\chi_{23}^\ell|^2 + |\chi_{32}^\ell|^2) \cos^2(\beta - \alpha) (1 + \tan^2 \beta)$$



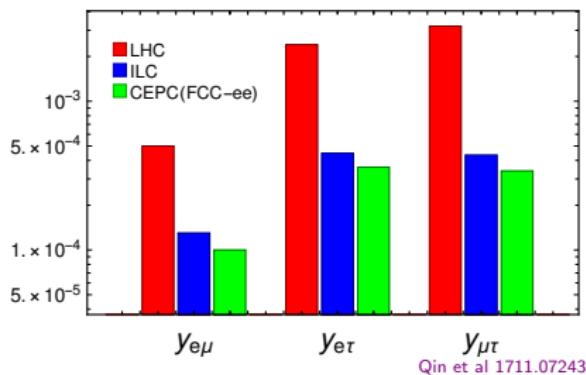
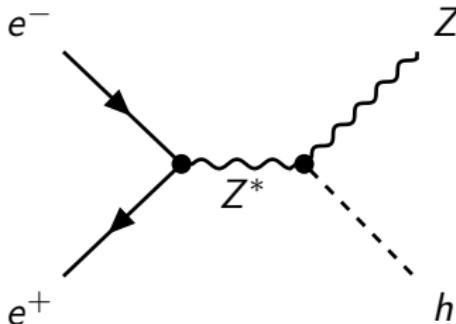
Example: Zee model

- Non-zero neutrino masses
- generated at loop level [Zee 1980](#)
- Simplest model with 2 Higgs doublets and charged singlet scalar h^+



[see [Herrero-Garcia et al 1605.06091](#) for Higgs cLFV in other neutrino mass models]

Future lepton collider

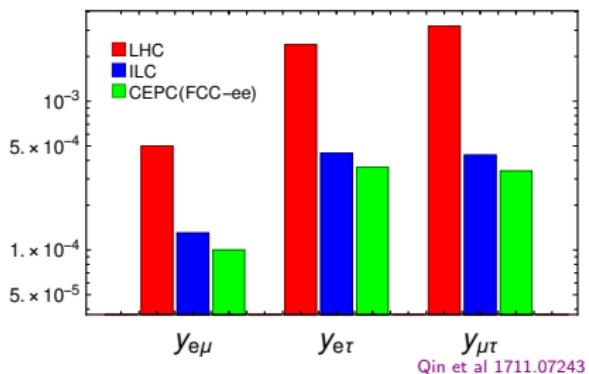
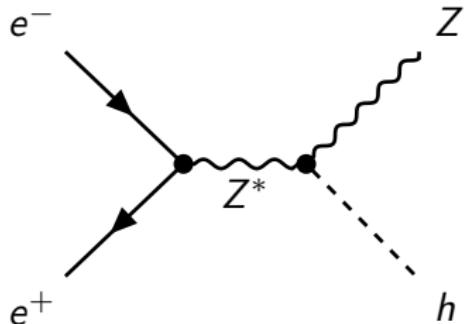


LHC CMS-PAS-HIG-16-005, CMS 1607.03561

ILC $\sqrt{s} = 250$ GeV, 4 polarizations, $\mathcal{L} = 2 \text{ ab}^{-1}$

CEPC $\sqrt{s} = 240$ GeV, $\mathcal{L} = 5 \text{ ab}^{-1}$

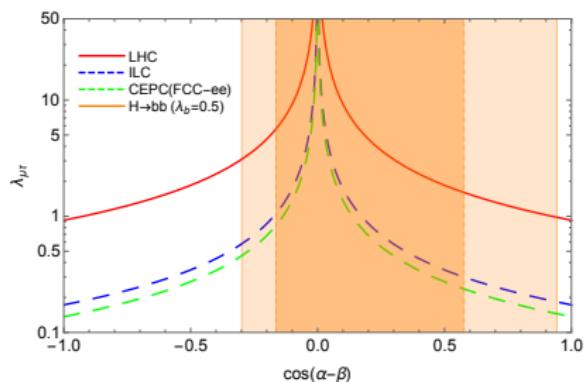
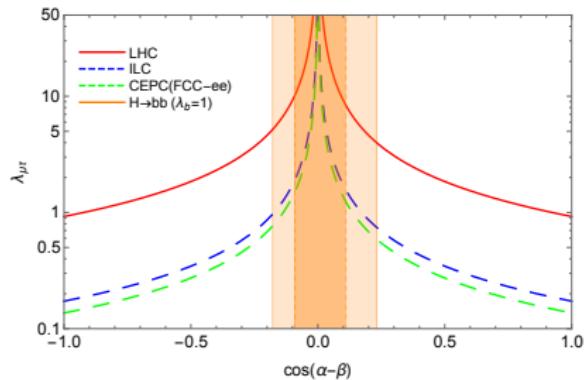
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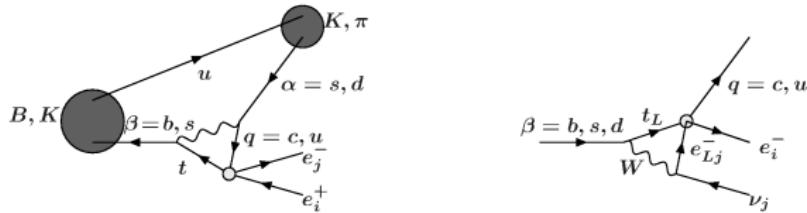
Top-quark decay

cLFV top-quark [Davidson et al 1507.07163]

described by D6 operators with **1 top quark** and **2 charged leptons**

$$\mathcal{L} = 2\sqrt{2}G_F \sum_i \epsilon_i \mathcal{O}_i$$

e.g. $\mathcal{O}_{LL,RR,LR,RL}^{AV} = (\bar{\ell}_i \gamma^\alpha P_X \ell_j)(\bar{u}_q \gamma_\alpha P_Y t)$



Davidson et al 1507.07163

- HERA $\sigma(e^\pm p \rightarrow e^\pm t + X) \leq 0.3 pb$
- $K \rightarrow e\mu, \mu \rightarrow e\gamma$
- radiative corrections

$e\mu$ op's: most $|\epsilon| \lesssim O(10^{-3} - 10^{-2})$, some $O(1)$

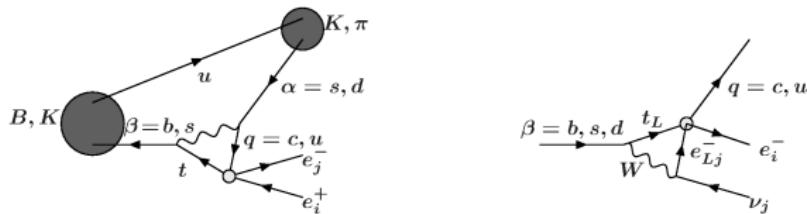
$\tau\ell$ op's $O(1 - 100)$ $|\epsilon_{S+P,L}^{ut}| \leq 0.03$

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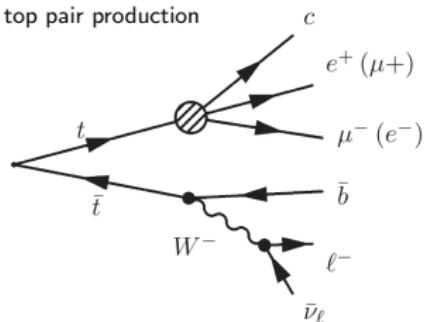
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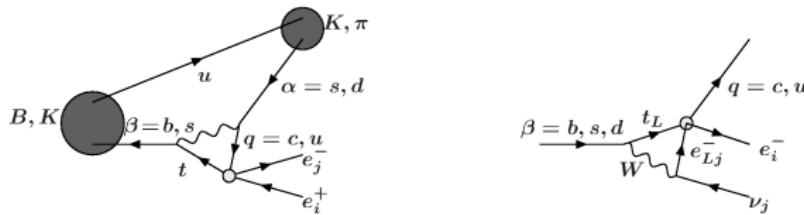


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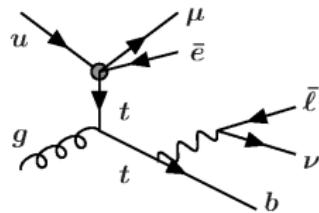
Davidson et al 1507.07163

single top quark production (more diag's)

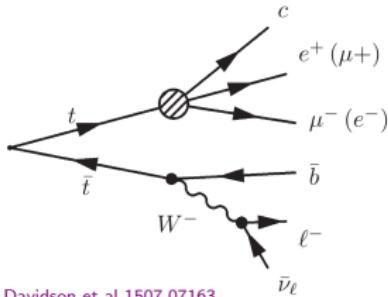
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$\tau\ell$ op's $O(1 - 100)$ $|\epsilon_{S+P,L}^{ut}| \leq 0.03$



cLFV top quark decay: top-quark pair production



Davidson et al 1507.07163

cross section

$$\sigma = 2\sigma_{t\bar{t}} BR(t \rightarrow \ell\nu b) \times BR(t \rightarrow \ell^\pm \ell'^\mp q)$$

$$BR(t \rightarrow \ell^\pm \ell'^\mp + q) \simeq 0.0027 \sum_{X,Y} |\epsilon_{XY}|^2$$

Main backgrounds:

- $t\bar{t}$ with non-prompt lepton
- $Z + \text{jets}$

Multi-variate analysis w/ 13 var's using BDT

observed [expected] limit

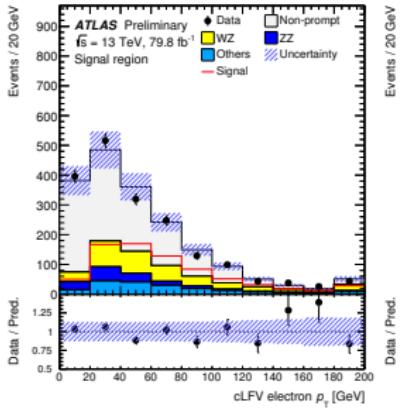
$$BR(t \rightarrow \ell\ell'q) < 1.86[1.36^{+0.61}_{-0.37}] \times 10^{-5}$$

$$BR(t \rightarrow e\mu q) < 6.6[4.8^{+2.1}_{-1.4}] \times 10^{-5}$$

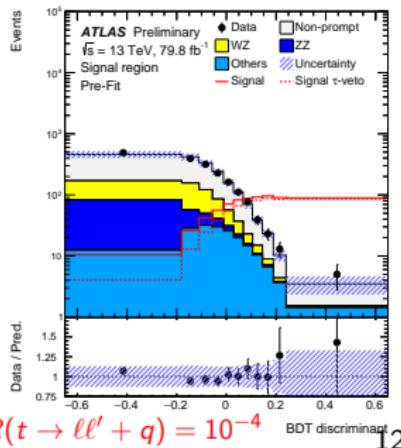
$\rightarrow |\epsilon| \lesssim 0.1$, more stringent for $t \rightarrow \tau + X$

low-energy lim's stronger for most $e\mu$ op's: $\epsilon_{LL,RL}$,

$\epsilon_{S\pm P,R}$, $\epsilon_{T,R}$

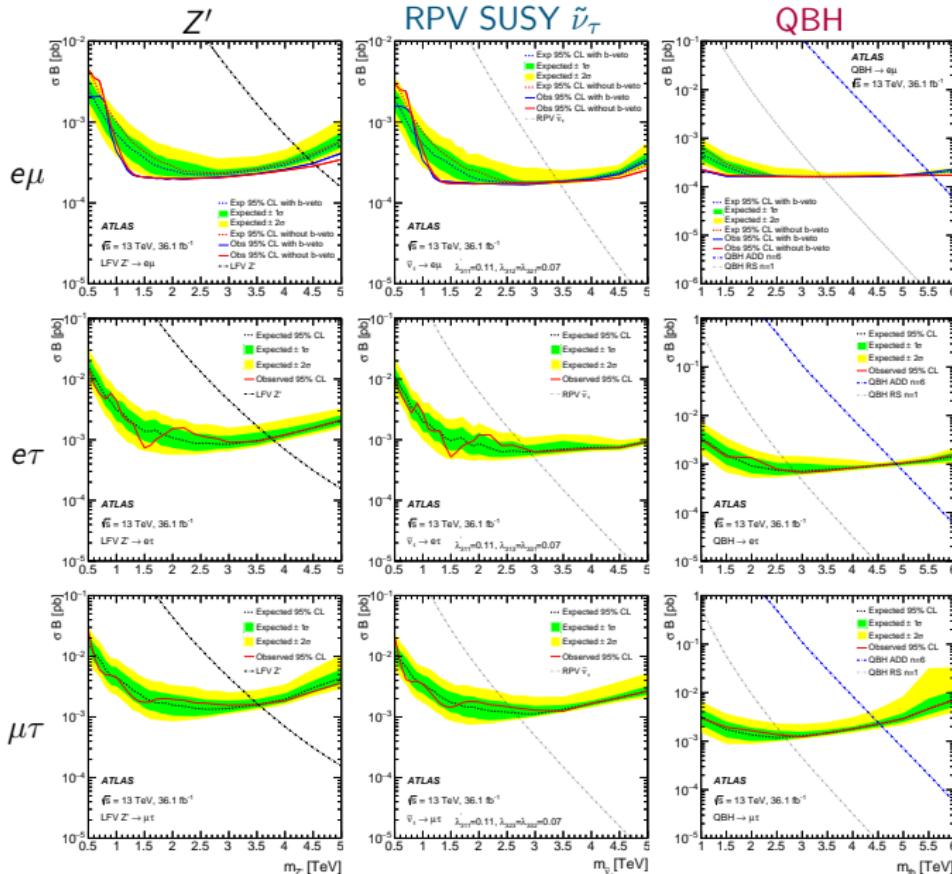


ATLAS-CONF-2018-044



Heavy resonance decay

Heavy resonance: Z' , RPV SUSY $\tilde{\nu}_\tau$, quantum black hole



$$Z'$$

$$Q_{ij} = \frac{g_{ij}}{g_{Z,SM}}$$

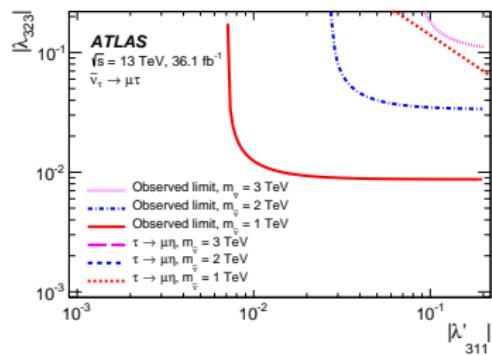
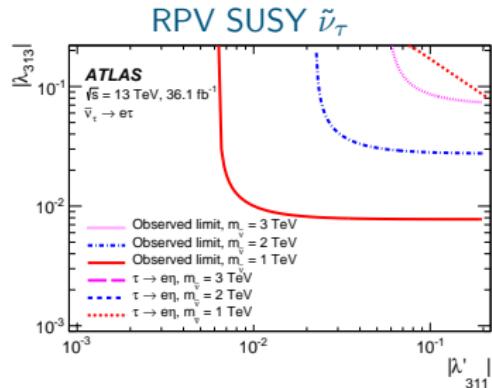
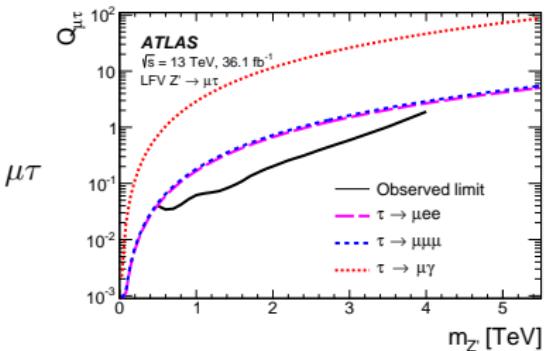
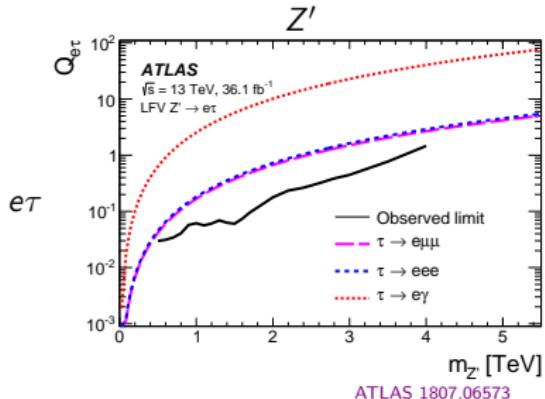
$$\text{RPV SUSY } \tilde{\nu}_\tau$$

$$W = \frac{1}{2} \lambda_{ijk} L_i L_j E_k^c + \lambda'_{ijk} L_i Q_j D_k^c$$

QBH
ADD (universal ED)
RS (warped ED)
 n number of ED

ATLAS 1807.06573

Heavy resonance: Z' , RPV SUSY $\tilde{\nu}_\tau$ cont.



$$Q_{ij} = \frac{g_{ij}}{g_{Z,SM}}$$

$$W = \frac{1}{2} \lambda_{ijk} L_i L_j E_k^c + \lambda'_{ijk} L_i Q_j D_k^c$$

Scattering at the LHC

D6 Operators with 2 Quarks and 2 Leptons

Buchmüller, Wyler NPB268(1986)621; Grzadkowski et al 1008.4884; Carpentier, Davidson 1008.0280; Petrov,Zhuridov 1308.6561

Vector

$$\begin{aligned} \mathcal{Q}_{lq}^{(1)} &= (\bar{L}\gamma_\mu L)(\bar{Q}\gamma^\mu Q) & \mathcal{Q}_{lq}^{(3)} &= (\bar{L}\gamma_\mu \tau^I L)(\bar{Q}\gamma^\mu \tau^I Q) \\ \mathcal{Q}_{eu} &= (\bar{\ell}\gamma_\mu \ell)(\bar{u}\gamma^\mu u) & \mathcal{Q}_{ed} &= (\bar{\ell}\gamma_\mu \ell)(\bar{d}\gamma^\mu d) \\ \mathcal{Q}_{lu} &= (\bar{L}\gamma_\mu L)(\bar{u}\gamma^\mu u) & \mathcal{Q}_{ld} &= (\bar{L}\gamma_\mu L)(\bar{d}\gamma^\mu d) \\ \mathcal{Q}_{qe} &= (\bar{Q}\gamma_\mu Q)(\bar{\ell}\gamma^\mu \ell) \end{aligned}$$

Scalar $\mathcal{Q}_{ledq} = (\bar{L}^\alpha \ell)(\bar{d} Q^\alpha)$ $\mathcal{Q}_{lequ}^{(1)} = (\bar{L}^\alpha \ell)\epsilon_{\alpha\beta}(\bar{Q}^\beta u)$

with same-flavour quark

Tensor $\mathcal{Q}_{lequ}^{(3)} = (\bar{L}^\alpha \sigma_{\mu\nu} \ell)\epsilon_{\alpha\beta}(\bar{Q}^\beta \sigma^{\mu\nu} u)$

D8 Operators with 2 Gluons and 2 Leptons

$$\begin{aligned} \mathcal{O}_X^{ij} &= \alpha_s G_{\mu\nu}^a G^{a\mu\nu} (\bar{e}_{Ri} L_j \cdot \phi^* + h.c.) & \mathcal{O}_X'^{ij} &= i \alpha_s G_{\mu\nu}^a \tilde{G}^{a\mu\nu} (\bar{e}_{Ri} L_j \cdot \phi^* - h.c.) \\ \bar{\mathcal{O}}_X^{ij} &= i \alpha_s G_{\mu\nu}^a G^{a\mu\nu} (\bar{e}_{Ri} L_j \cdot \phi^* - h.c.) & \bar{\mathcal{O}}_X'^{ij} &= \alpha_s G_{\mu\nu}^a \tilde{G}^{a\mu\nu} (\bar{e}_{Ri} L_j \cdot \phi^* + h.c.) \\ \mathcal{O}_Y^{ij} &= i \alpha_s G_{\mu\rho}^a G_{\sigma\nu}^a \eta^{\rho\sigma} \bar{L}_i \gamma^\mu D^\nu L_j & \mathcal{O}_Z^{ij} &= i \alpha_s G_{\mu\rho}^a G_{\sigma\nu}^a \eta^{\rho\sigma} \bar{e}_{Ri} \gamma^\mu D^\nu e_{Rj} \end{aligned}$$

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Buchmüller, Wyler NPB268(1986)621; Grzadkowski et al 1008.4884; Carpentier, Davidson 1008.0280; Petrov,Zhuridov 1308.6561

Vector

$$\begin{array}{ll} \mathcal{Q}_{lq}^{(1)} = (\bar{L}\gamma_\mu L)(\bar{Q}\gamma^\mu Q) & \mathcal{Q}_{lq}^{(3)} = (\bar{L}\gamma_\mu \tau^I L)(\bar{Q}\gamma^\mu \tau^I Q) \\ \mathcal{Q}_{eu} = (\bar{\ell}\gamma_\mu \ell)(\bar{u}\gamma^\mu u) & \mathcal{Q}_{ed} = (\bar{\ell}\gamma_\mu \ell)(\bar{d}\gamma^\mu d) \\ \mathcal{Q}_{lu} = (\bar{L}\gamma_\mu L)(\bar{u}\gamma^\mu u) & \mathcal{Q}_{ld} = (\bar{L}\gamma_\mu L)(\bar{d}\gamma^\mu d) \\ \mathcal{Q}_{qe} = (\bar{Q}\gamma_\mu Q)(\bar{\ell}\gamma^\mu \ell) & \end{array}$$

Scalar $\mathcal{Q}_{ledq} = (\bar{L}^\alpha \ell)(\bar{d} Q^\alpha)$ $\mathcal{Q}_{lequ}^{(1)} = (\bar{L}^\alpha \ell)\epsilon_{\alpha\beta}(\bar{Q}^\beta u)$

with same-flavour quark

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D8 Operators with 2 Gluons and 2 Leptons

$$\begin{array}{ll} \mathcal{O}_X^{ij} = \alpha_s G_{\mu\nu}^a G^{a\mu\nu} (\bar{e}_{Ri} L_j \cdot \phi^* + h.c.) & \mathcal{O}_X'^{ij} = i \alpha_s G_{\mu\nu}^a \tilde{G}^{a\mu\nu} (\bar{e}_{Ri} L_j \cdot \phi^* - h.c.) \\ \bar{\mathcal{O}}_X^{ij} = i \alpha_s G_{\mu\nu}^a G^{a\mu\nu} (\bar{e}_{Ri} L_j \cdot \phi^* - h.c.) & \bar{\mathcal{O}}_X'^{ij} = \alpha_s G_{\mu\nu}^a \tilde{G}^{a\mu\nu} (\bar{e}_{Ri} L_j \cdot \phi^* + h.c.) \\ \mathcal{O}_Y^{ij} = i \alpha_s G_{\mu\rho}^a G_{\sigma\nu}^a \eta^{\rho\sigma} \bar{L}_i \gamma^\mu D^\nu L_j & \mathcal{O}_Z^{ij} = i \alpha_s G_{\mu\rho}^a G_{\sigma\nu}^a \eta^{\rho\sigma} \bar{e}_{Ri} \gamma^\mu D^\nu e_{Rj} \end{array}$$

D6 Operators with 2 Quarks and 2 Leptons

Buchmüller, Wyler NPB268(1986)621; Grzadkowski et al 1008.4884; Carpentier, Davidson 1008.0280; Petrov,Zhuridov 1308.6561

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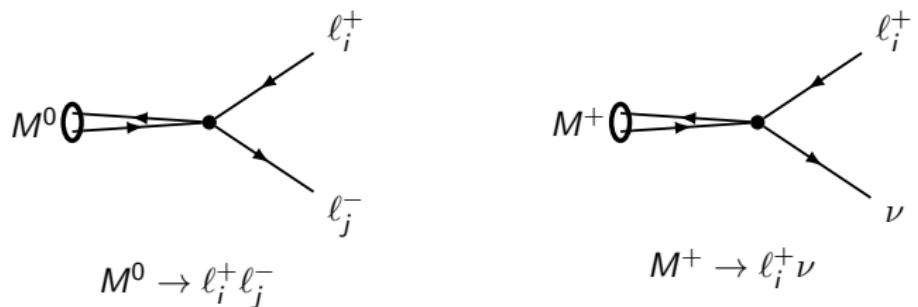
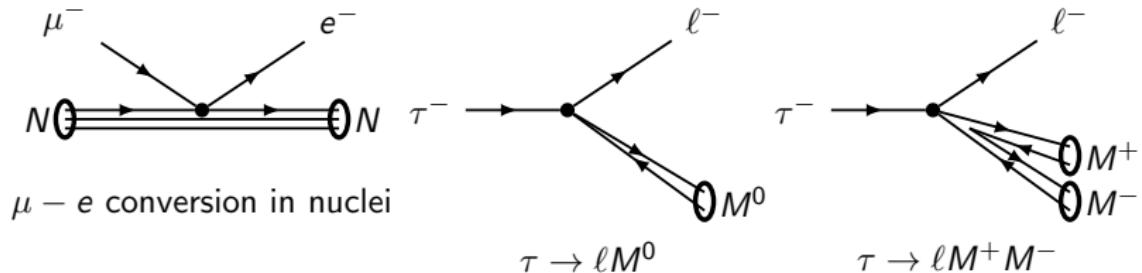
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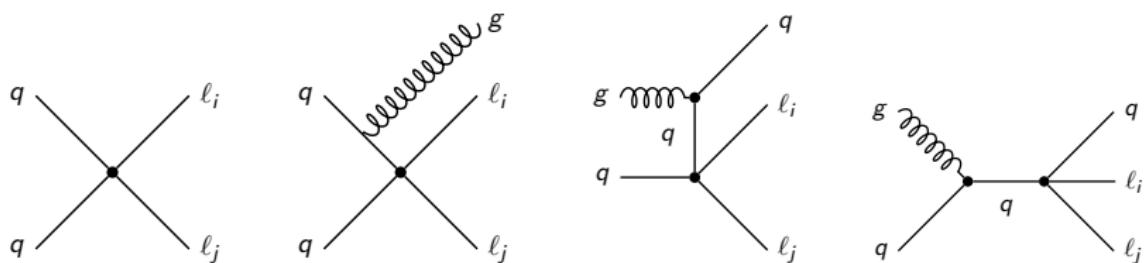
Precision Experiments

[Cai, MS 1510.02486]



Processes at LHC:

$$pp \rightarrow \ell_i \ell_j + \text{jets}$$



Signal: opposite-sign different flavour pair of leptons

Several existing searches:

- ATLAS 7 TeV: LFV heavy neutral particle decay to $e\mu$ [ATLAS 1103.5559](#)
- CMS 8 TeV: LFV heavy neutral particle decay to $e\mu$ [CMS-PAS-EXO-13-002](#)
- **ATLAS 7 TeV: LFV in $e\mu$ continuum in R'SUSY** [ATLAS 1205.0725](#)
- **ATLAS 8 TeV: LFV heavy neutral particle decay** [ATLAS 1503.04430](#)
- CMS 8 TeV: LFV heavy neutral particle decay to $e\mu$ [CMS 1604.05239](#)
- ATLAS 13 TeV, 3.2 fb^{-1} : LFV heavy neutral particle decay [ATLAS 1607.08079](#)
- ATLAS 13 TeV, 36.1 fb^{-1} [ATLAS 1807.06573](#)

Recast limits of most sensitive previous searches

ATLAS 1503.04430	ATLAS 1205.0725
8 TeV	7 TeV
20.3 fb^{-1}	2.1 fb^{-1}
$e\mu, e\tau, \mu\tau$	$e\mu$
inclusive	exclusive
including arbitrary number of jets	separated by number of jets

Projection to 14 TeV

- Assuming 300 fb^{-1}
- Follow searching strategy of exclusive 7 TeV search

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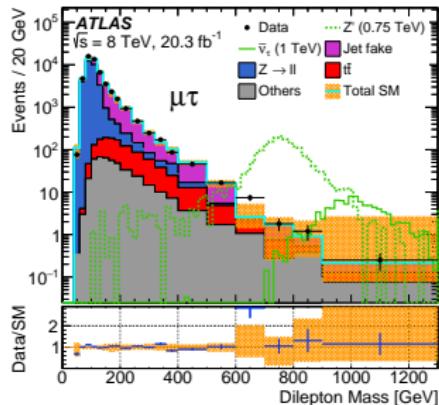
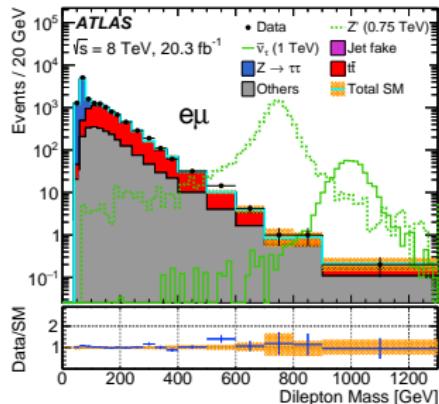
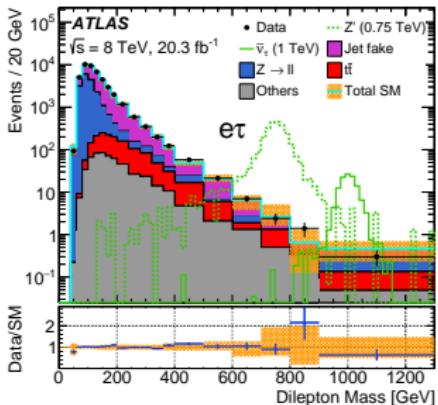
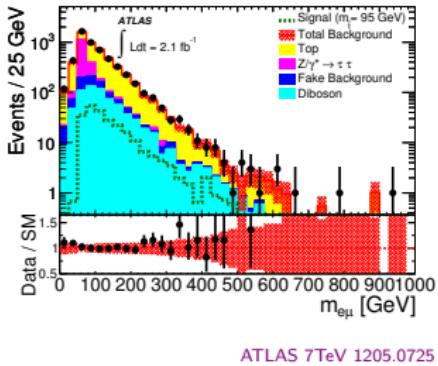
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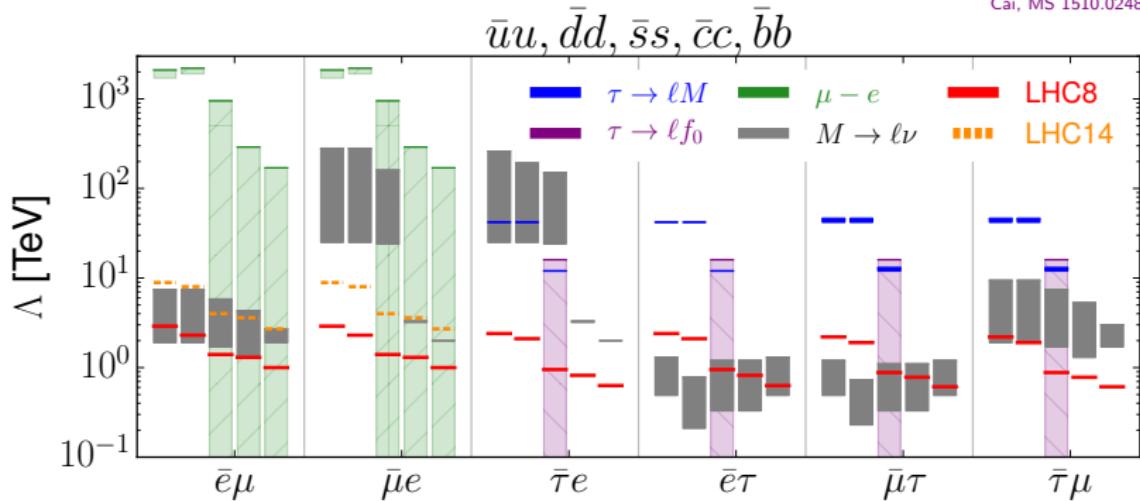
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ATLAS Searches [Cai, MS 1510.02486]



cLFV at hadron colliders: quarks

Cai, MS 1510.02486



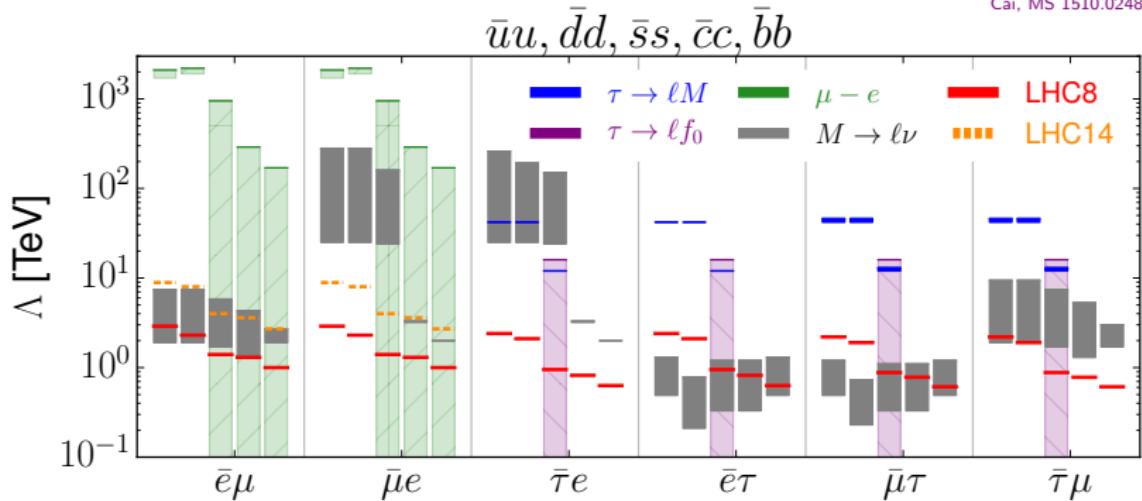
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LHC more interesting for vector operators with right-handed quark currents due to weaker constraints from intensity frontier

$$[\bar{q}\gamma_\mu P_R q][\bar{\ell}\gamma_\mu P_{R,L} \ell]$$

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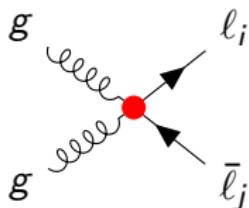


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Processes at LHC: $pp \rightarrow \ell_i \ell_j$



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opposite-sign different flavour pair of leptons

Most sensitive searches

ATLAS 1607.08079 CMS-PAS-EXO-16-058 1802.01122

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newer ATLAS search: 13 TeV, 36.1 fb^{-1} 1807.06573

EFT scattering amplitudes

$$\mathcal{A}(s) \simeq \frac{s}{\Lambda^2} \xrightarrow{s \rightarrow \infty} \infty$$

\Rightarrow Violation of perturbative unitarity

Solutions:

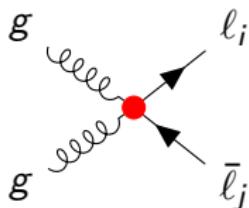
- UV-complete models/simplified models
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Wigner 1964; Wigner, Eisenbud 1947; Gupta 1950
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Baur, Zeppenfeld hep-ph/9309227

$$C \rightarrow \frac{C}{1 + \frac{s}{\Lambda^2}}$$

cLFV at the Large Hadron Collider (LHC): gluons [Cai, MS, Valencia 1802.09822]

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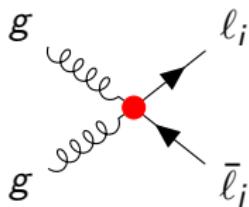
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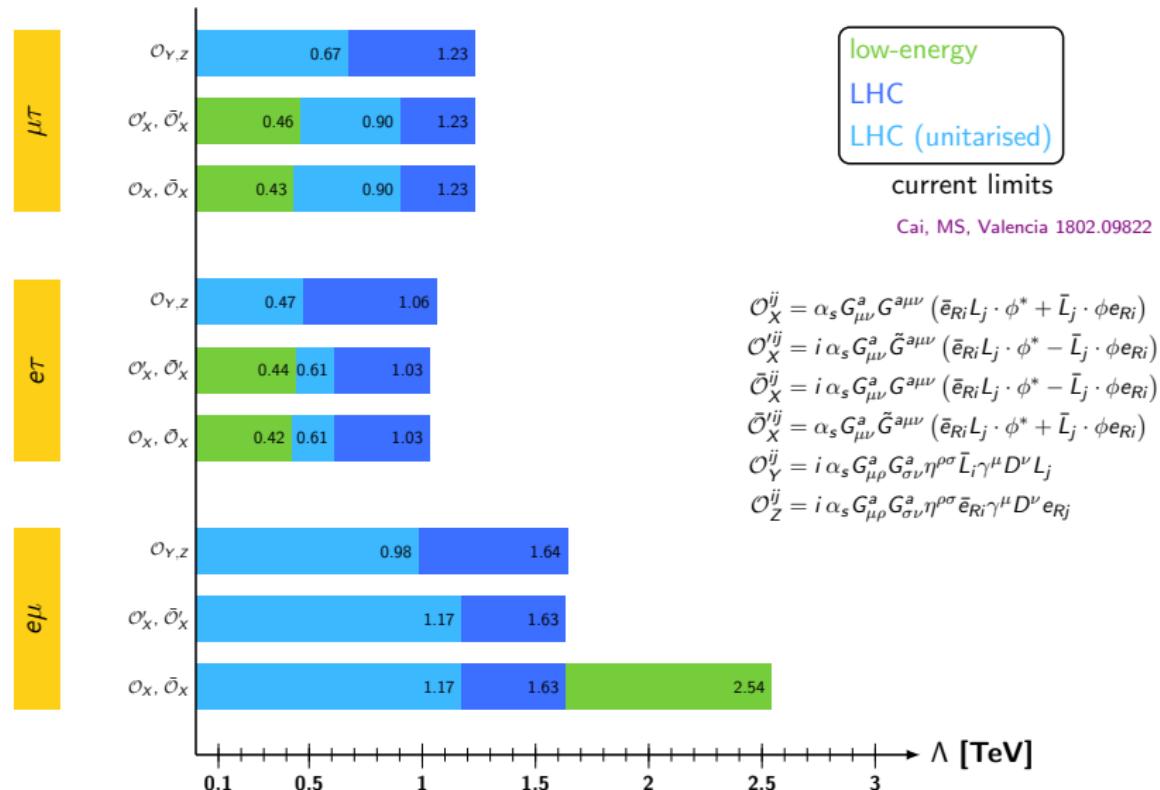
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cLFV at hadron colliders: gluons



See also Bhattacharya et al 1802.06082 for a related analysis

Scattering at future lepton colliders

Bileptons - seven simplified models [Li,MS 1809.07924]

$$\Delta L = 0$$

complex scalar $H_2 \sim (2, \frac{1}{2})$

$$\mathcal{L} = y_2^{ij} \textcolor{red}{H}_2 \bar{L}_i P_R \ell_j + h.c.$$

LH singlet vector $H_1 \sim (1, 0)$

$$\mathcal{L} = y_1^{ij} \textcolor{red}{H}_{1\mu} \bar{L}_i \gamma^\mu P_L L_j$$

LH triplet vector $H_3 \sim (3, 0)$

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assumption: real and symmetric
Yukawa coupling matrices

related work: Dev, Mohapatra, Zhang 1711.08430, also 1712.03642, 1803.11167

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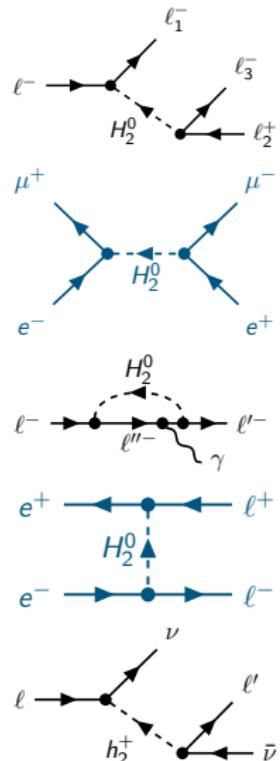
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Existing (low-energy) precision constraints [Li,MS 1809.07924]

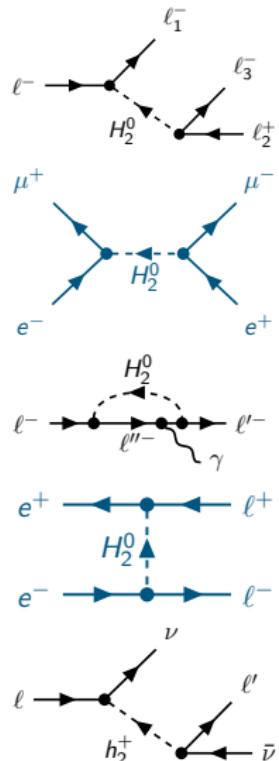
- LFV trilepton decays, $\ell \rightarrow \ell_1 \bar{\ell}_2 \bar{\ell}_3$
- Muonium antimuonium conversion,
 $\mu^+ e^- \rightarrow \mu^- e^+$
- anomalous magnetic (and electric) dipole moments, a_ℓ
- LEP/LHC searches
- lepton flavour non-universality, $\ell \rightarrow \ell' \nu \bar{\nu}$



Future sensitivity improvements at e.g. Belle 2, Mu3E, ...

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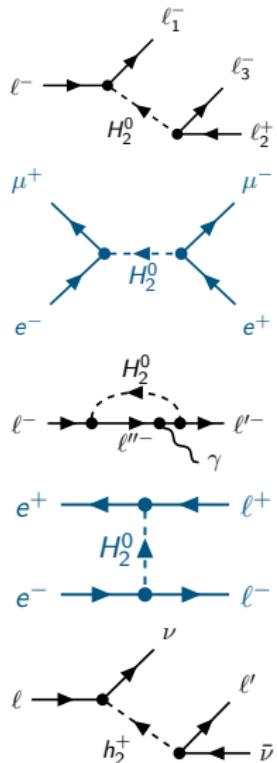
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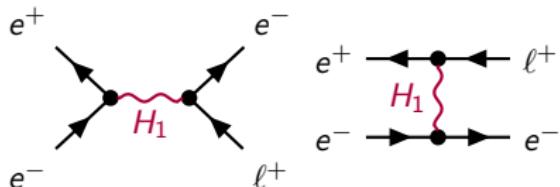
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Off-shell production $H_{1\mu}$: $e^+e^- \rightarrow e^\pm\mu^\mp(e^\pm\tau^\mp)$ [Li,MS 1809.07924]

$$\mathcal{L} = y_1^{ij} H_{1\mu} \bar{L}_i \gamma^\mu P_L L_j$$



Basic cuts: $p_T > 10$ GeV and $|\eta| < 2.5$

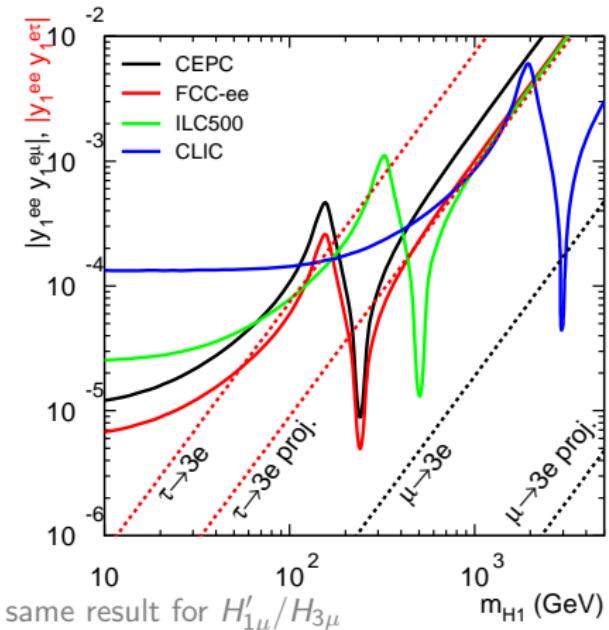
Four collider configurations:

CEPC: 5 ab^{-1} at 240 GeV

FCC-ee: 16 ab^{-1} at 240 GeV

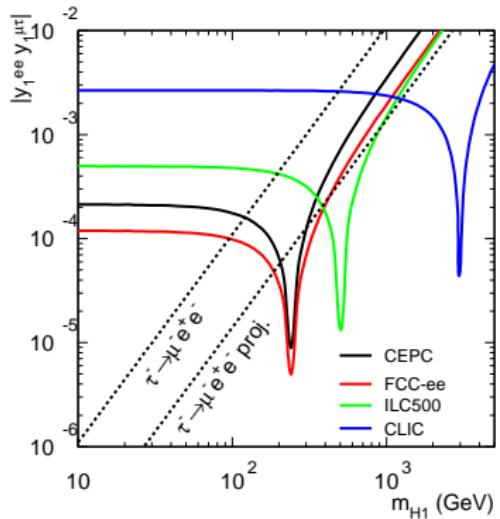
ILC500: 4 ab^{-1} at 500 GeV

CLIC: 5 ab^{-1} at 3 TeV

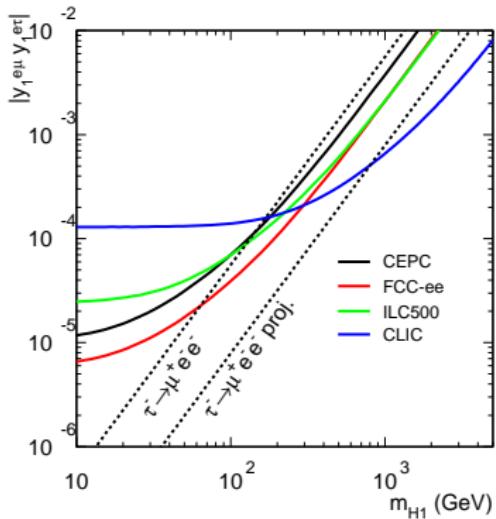
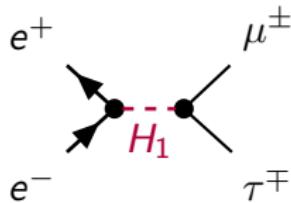


τ efficiency not included in figure

60% τ eff. \Rightarrow 77% sensitivity reduction for 1 τ

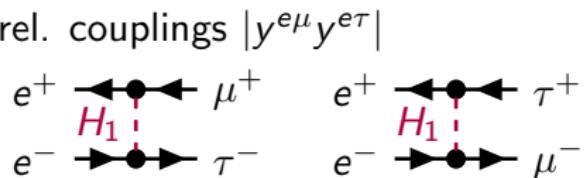
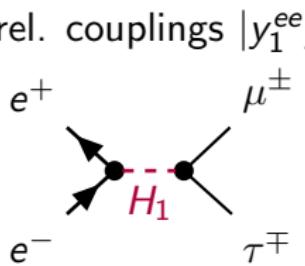
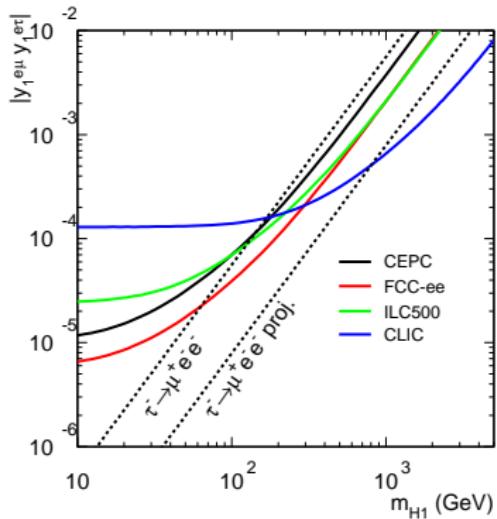
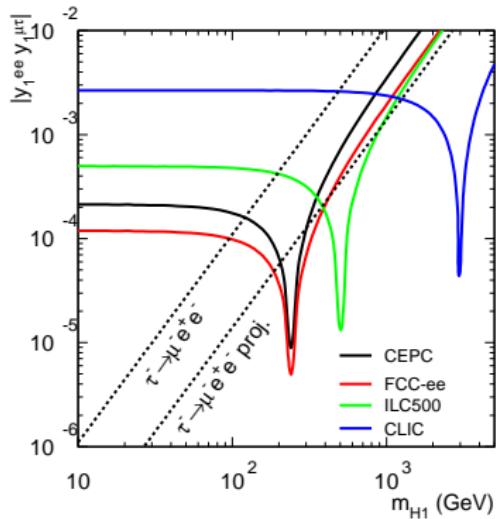


rel. couplings $|y_1^{ee} y_1^{\mu\tau}|$

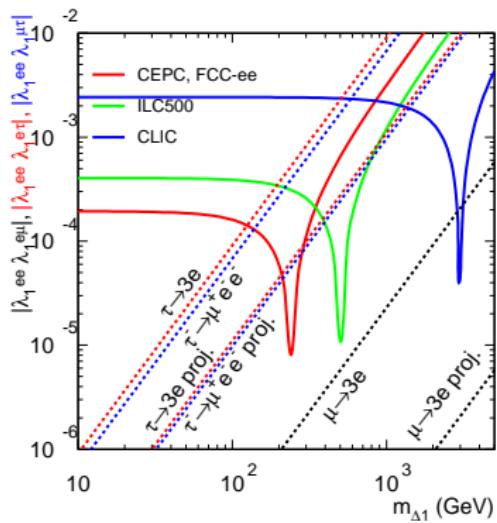
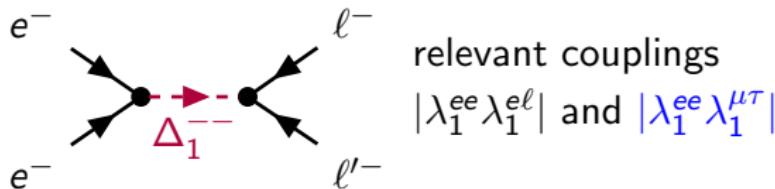


rel. couplings $|y_1^{e\mu} y_1^{e\tau}|$





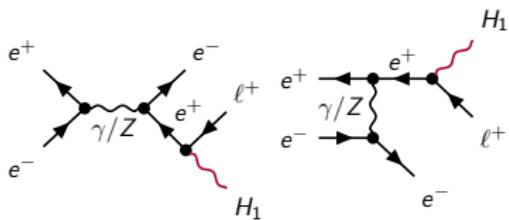
Same-sign lepton collider - Δ_1 : $e^- e^- \rightarrow \ell^- \ell'^-$ [Li,MS 1809.07924]



smaller integrated luminosity
 $\mathcal{L} = 500 \text{ fb}^{-1}$

On-shell production $H_{1\mu}$: $e^+e^- \rightarrow e^\pm\mu^\mp(e^\pm\tau^\mp) + H_1$ [Li,MS in preparation]

$$\mathcal{L} = y_1^{ij} H_{1\mu} \bar{L}_i \gamma^\mu P_L L_j + y_3^{ij} \bar{L}_i \gamma^\mu \vec{\sigma} \cdot H_{3\mu} P_L L_j$$



Cuts: $p_T > 10$ GeV and $|\eta| < 2.5$

Five collider configurations:

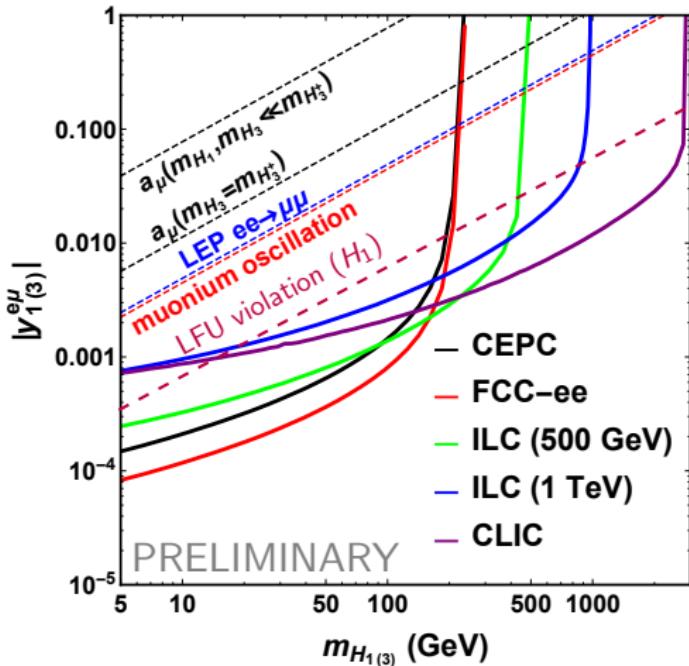
CEPC: 5 ab^{-1} at 240 GeV

FCC-ee: 16 ab^{-1} at 240 GeV

ILC (500 GeV): 4 ab^{-1} at 500 GeV

ILC (1TeV): 1 ab^{-1} at 1 TeV

CLIC: 5 ab^{-1} at 3 TeV



τ efficiency not included in figure

60% τ eff. \Rightarrow 77% sensitivity reduction for 1 τ

Conclusions

Conclusions

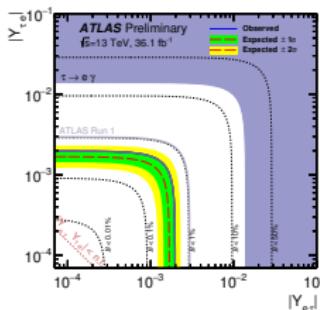
colliders complementary way to search for charged LFV

$\mu \leftrightarrow e$ flavour: stringent limits from low-energy precision exp.

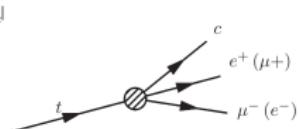
$\tau \leftrightarrow \ell$ flavour complementary sensitivity at colliders

colliders test more Lorentz structures

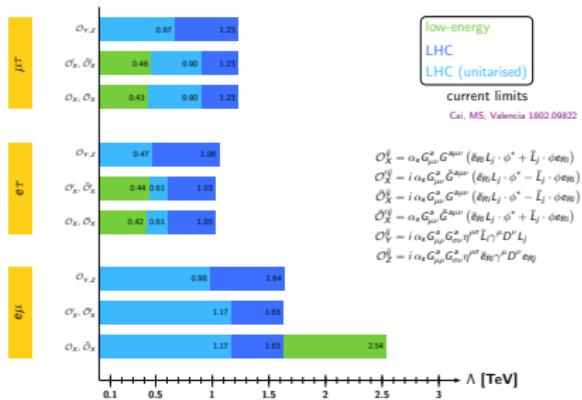
best for operators which are difficult to constrain at low energy



cLFV Higgs decay

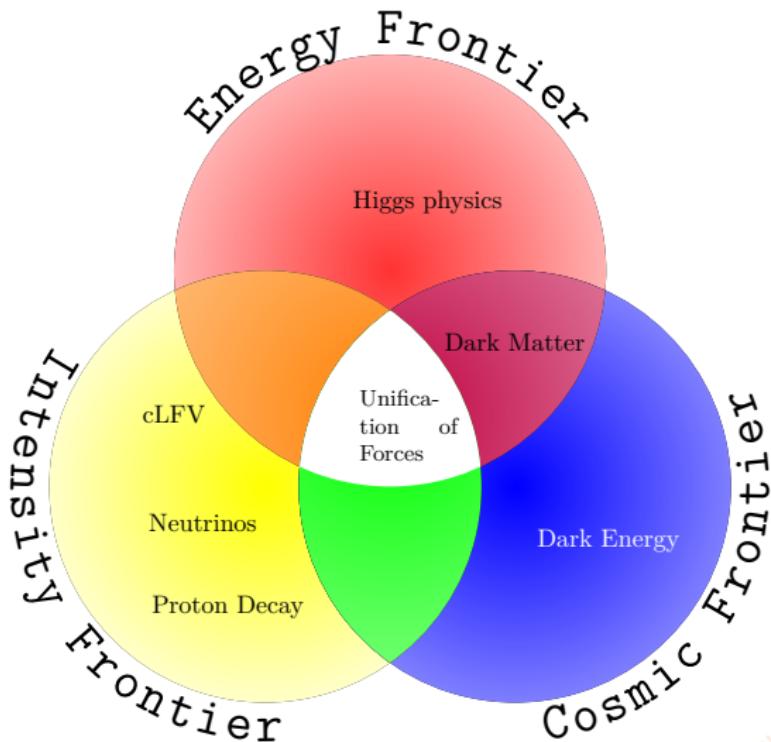


cLFV top decay



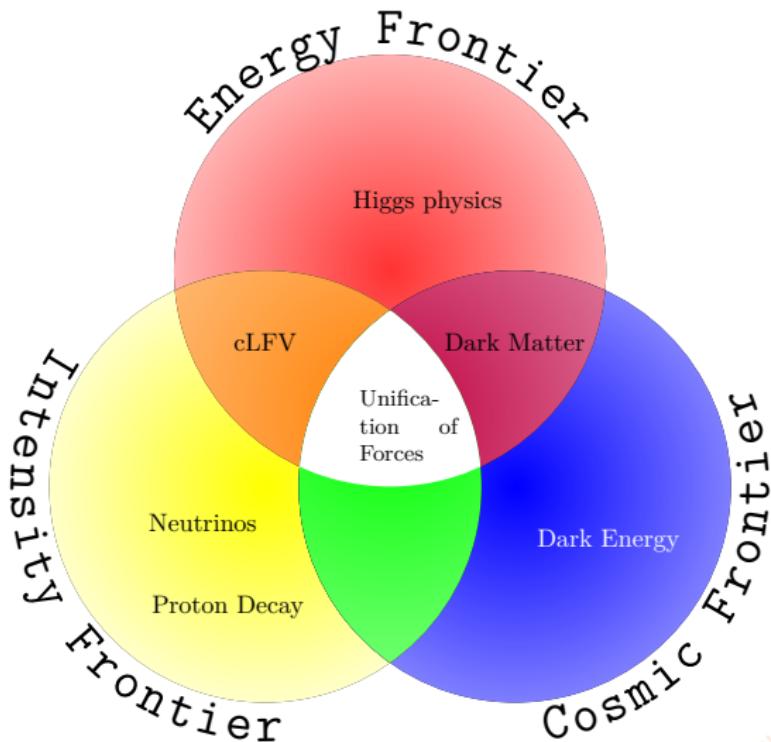
cLFV scattering with initial state gluons

Conclusions cont.



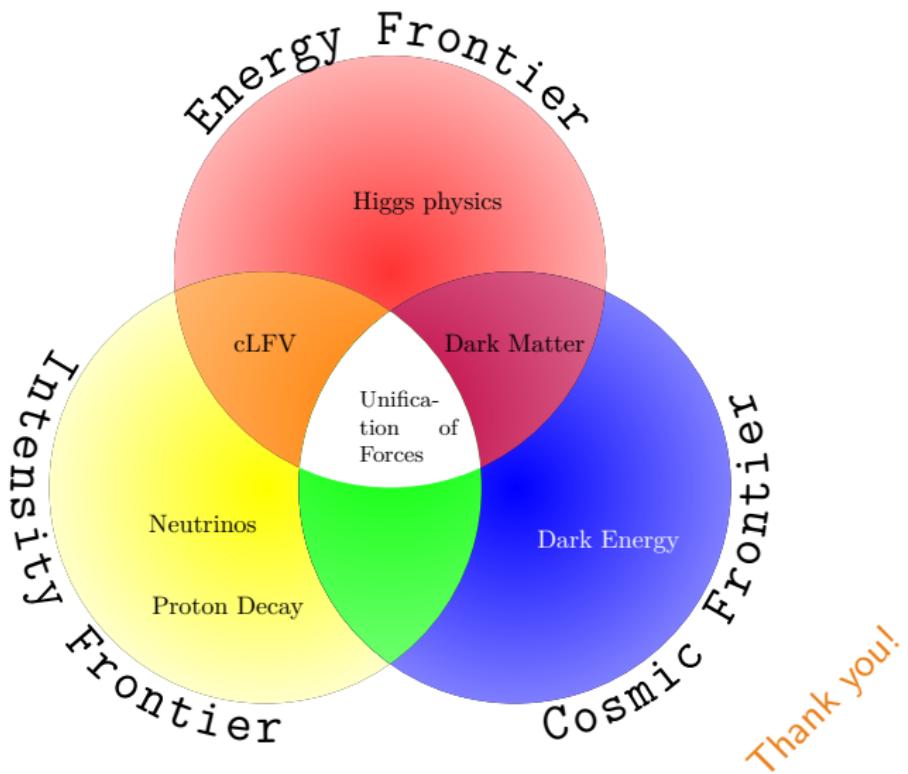
Thank you!

Conclusions cont.



Thank you!

Conclusions cont.



Backup slides

Scalar Operators

$$\mathcal{Q}_{ledq} = (\bar{L}^\alpha \ell)(\bar{d} Q^\alpha) \quad \mathcal{Q}_{lequ}^{(1)} = (\bar{L}^\alpha \ell)\epsilon_{\alpha\beta}(\bar{Q}^\beta u)$$

Relevant Wilson coefficients $\Xi^{u,d}$ of SM EFT

$$-\mathcal{L} = \Xi_{ij,kk}^d (\mathcal{Q}_{ledq})_{ij,kk} + \Xi_{ij,kk}^u (\mathcal{Q}_{lequ}^{(1)})_{ij,kk} + \text{h.c.} .$$

Effective four fermion Lagrangian

$$\begin{aligned} \mathcal{L}_{4f} = & \Xi_{ij,kl}^{Cd} (\bar{\nu}_{Li} \ell_{Rj})(\bar{d}_{Rk} u_{LI}) + \Xi_{ij,kl}^{Nd} (\bar{\ell}_{Li} \ell_{Rj})(\bar{d}_{Rk} d_{LI}) \\ & + \Xi_{ij,kl}^{Cu} (\bar{\nu}_{Li} \ell_{Rj})(\bar{d}_{Lk} u_{RI}) + \Xi_{ij,kl}^{Nu} (\bar{\ell}_{Li} \ell_{Rj})(\bar{u}_{Lk} u_{RI}) . \end{aligned}$$

We do not consider top quark because of different phenomenology.

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Thus the most general four fermion coefficients are

$$\begin{aligned} \Xi_{ij,kl}^{Nd} &= U_{ii'}^{\ell*} V_{lk}^d \Xi_{ij,kk}^d & \Xi_{ij,kl}^{Cd} &= U_{ii'}^{\nu*} V_{lk}^u \Xi_{i'j,kk}^d \\ \Xi_{ij,kl}^{Nu} &= -U_{ii'}^{\ell*} V_{kl}^{u*} \Xi_{ij,II}^u & \Xi_{ij,kl}^{Cu} &= U_{ii'}^{\nu*} V_{kl}^{d*} \Xi_{i'j,II}^u \end{aligned}$$

In general there is quark flavour violation.

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Scalar Operators

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Choose basis in which charged lepton mass matrix is diagonal as well as $\Xi_{ij,kk}^{N?}$

$$\begin{aligned}\Xi_{ij,kl}^{Nd} &= \delta_{kl} \Xi_{ij,kk}^d & \Xi_{ij,kl}^{Cd} &= U_{ii'}^* V_{kl}^* \Xi_{i'j,kk}^d \\ \Xi_{ij,kl}^{Nu} &= -\delta_{kl} \Xi_{ij,kk}^u & \Xi_{ij,kl}^{Cu} &= U_{ii'}^* V_{kl}^* \Xi_{i'j,II}^u\end{aligned}$$

\Rightarrow No tree-level FCNC processes.

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Scalar Operators

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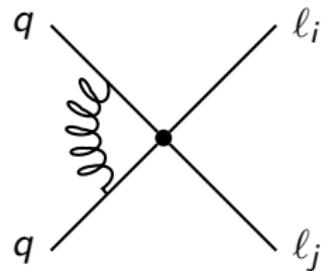
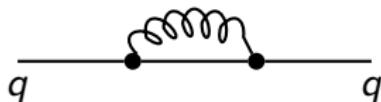
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Renormalization Group Corrections

- Main effect are QCD corrections



- Following the standard discussion at NLO

Buchalla,Buras, Lautenbacher hep-ph/9512380

$$\Xi(\mu) = \Xi(\mu_0) \left(\frac{\alpha_s(\mu)}{\alpha_s(\mu_0)} \right)^{\frac{\gamma_0}{2\beta_0}}$$

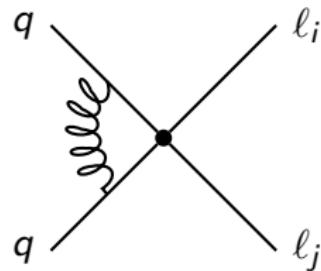
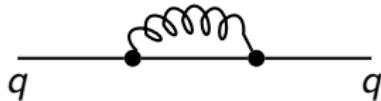
with coefficients

$$\beta_0 = 11 - 2n_F/3 \quad \text{and} \quad \gamma_0 = 6C_2(3) = 8$$

- Wilson coefficients become larger at smaller scales.
⇒ Increases reach of precision experiments

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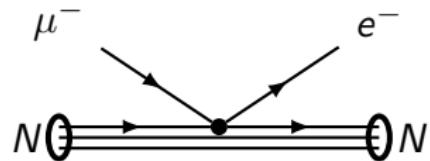
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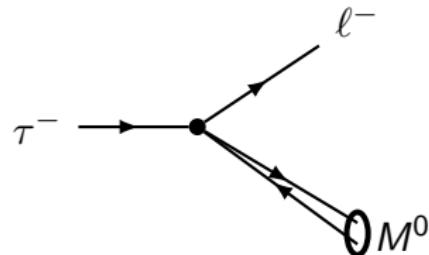
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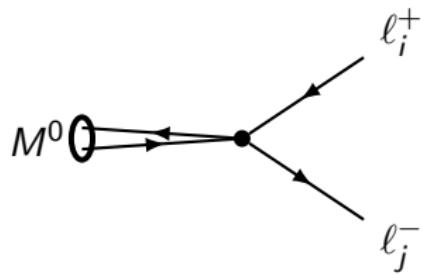
Precision Experiments



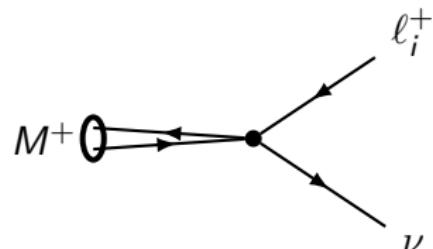
$\mu - e$ conversion in nuclei



$$\tau \rightarrow \ell M^0$$



$$M^0 \rightarrow \ell_i^+ \ell_j^-$$

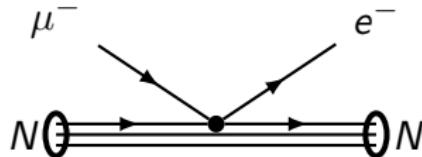


$$M^+ \rightarrow \ell_i^+ \nu$$

$\mu - e$ Conversion

- Agnostic about mediation mechanism
- Following discussion in

Gonzalez, Gutsche, Helo, Kovalenko, Lyubovitskij, Schmidt 1303.0596



Dimensionless $\mu - e$ conversion rate

$$R_{\mu e}^{(A,Z)} \equiv \frac{\Gamma(\mu^- + (A, Z) \rightarrow e^- + (A, Z))}{\Gamma(\mu^- + (A, Z) \rightarrow \nu_\mu + (A, Z - 1))}$$

with muon conversion rate

$$\Gamma(\mu^- + (A, Z) \rightarrow e^- + (A, Z)) = \left| \Xi_{ij,kl}^{Nu, Nd} \right|^2 \times \mathcal{F} \times \frac{p_e E_e (\mathcal{M}_p + \mathcal{M}_n)^2}{2\pi}$$

\mathcal{F} depends on mediation mechanism

No dependence on phase of Ξ if there is only one operator.

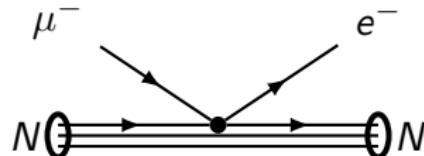
Strongest limit for first generation quarks,

but non-negligible for other quarks if pure direct nuclear mediation

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	^{48}Ti	^{197}Au	^{208}Pb
$R_{\mu e}^{\max}$	4.3×10^{-11}	7.0×10^{-13}	4.6×10^{-11}
$\bar{u}u$	1100 [870]	2100 [1700]	760 [610]
$\bar{d}d$	1100 [930]	2200 [1900]	780 [680]
$\bar{s}s$	480 [-]	950 [-]	340 [-]
$\bar{c}c$	150 [-]	290 [-]	110 [-]
$\bar{b}b$	84 [-]	170 [-]	61 [-]

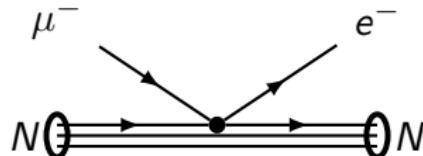
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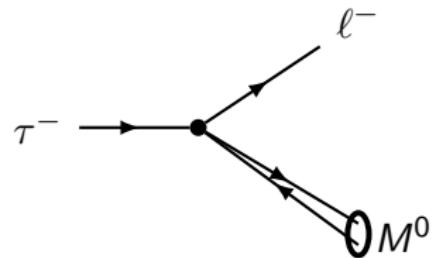
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LFV Semileptonic τ Decays

- Only light quarks u,d,s
- Weak dependence on phase
- f_0 : φ_m parameterises quark content
- Quark FCNC parameterised by λ

$$\Xi_{ij,kl}^u = \lambda \Xi_{ij,II}^u V_{kl} \quad \Xi_{ij,kl}^d = \lambda \Xi_{ij,kk}^d V_{kl}$$



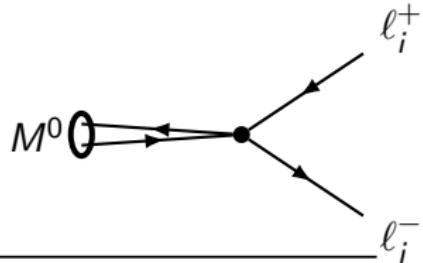
decay	Br_i^{\max}	cutoff scale Λ [TeV]		
		$\Xi_{ij,uu}^u$	$\Xi_{ij,dd}^d$	$\Xi_{ij,ss}^d$
$\tau^- \rightarrow e^- \pi^0$	8.0×10^{-8}	10	10	-
$\tau^- \rightarrow e^- \eta$	9.2×10^{-8}	34	34	7.9
$\tau^- \rightarrow e^- \eta'$	1.6×10^{-7}	42	42	12
$\tau^- \rightarrow e^- K_S^0$	2.6×10^{-8}	-	$7.8\sqrt{\lambda}$	$7.8\sqrt{\lambda}$
$\tau^- \rightarrow e^- (f_0(980) \rightarrow \pi^+ \pi^-)$	3.2×10^{-8}	$13\sqrt{\sin \varphi_m}$	$13\sqrt{\sin \varphi_m}$	$16\sqrt{\cos \varphi_m}$
$\tau^- \rightarrow \mu^- \pi^0$	1.1×10^{-7}	9.0 – 9.6	9.0 – 9.6	-
$\tau^- \rightarrow \mu^- \eta$	6.5×10^{-8}	36 – 38	36 – 38	8.4 – 8.9
$\tau^- \rightarrow \mu^- \eta'$	1.3×10^{-7}	42 – 46	42 – 46	12 – 13
$\tau^- \rightarrow \mu^- K_S^0$	2.3×10^{-8}	-	$(7.8 - 8.3)\sqrt{\lambda}$	$(7.8 - 8.3)\sqrt{\lambda}$
$\tau^- \rightarrow \mu^- (f_0(980) \rightarrow \pi^+ \pi^-)$	3.4×10^{-8}	$(12 - 14)\sqrt{\sin \varphi_m}$	$(12 - 14)\sqrt{\sin \varphi_m}$	$(15 - 16)\sqrt{\cos \varphi_m}$

Leptonic Neutral Meson Decays $M^0 \rightarrow \ell_i^+ \ell_j^-$

Quark FCNC parameterised by λ

$$\Xi_{ij,kl}^u = \lambda \Xi_{ij,II}^u V_{kl}$$

$$\Xi_{ij,kl}^d = \lambda \Xi_{ij,kk}^d V_{kl}$$

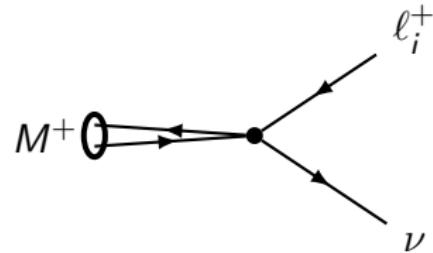


For $\lambda = 0$ only constraints from $\pi^0, \eta^{(\prime)}$ decays

decay	Br_i^{\max}	cutoff scale Λ [TeV]				
		$\Xi_{ij,uu}^u$	$\Xi_{ij,dd}^d$	$\Xi_{ij,ss}^d$	$\Xi_{ij,cc}^u$	$\Xi_{ij,bb}^d$
$\pi^0 \rightarrow \mu^+ e^-$	3.8×10^{-10}	2.2	2.2	-	-	-
$\pi^0 \rightarrow \mu^- e^+$	3.4×10^{-9}	1.2	1.2	-	-	-
$\pi^0 \rightarrow \mu^+ e^- + \mu^- e^+$	3.6×10^{-10}	2.6	2.6	-	-	-
$\eta \rightarrow \mu^+ e^- + \mu^- e^+$	6×10^{-6}	0.52	0.52	0.12	-	-
$\eta' \rightarrow e\mu$	4.7×10^{-4}	0.091	0.091	0.026	-	-
<hr/>						
$K_L^0 \rightarrow e^\pm \mu^\mp$	4.7×10^{-12}	-	$86\sqrt{\lambda}$	$86\sqrt{\lambda}$	-	-
$D^0 \rightarrow e^\pm \mu^\mp$	2.6×10^{-7}	$6.4\sqrt{\lambda}$	-	-	$6.4\sqrt{\lambda}$	-
$B^0 \rightarrow e^\pm \mu^\mp$	2.8×10^{-9}	-	$10\sqrt{\lambda}$	-	-	$6.6\sqrt{\lambda}$
$B^0 \rightarrow e^\pm \tau^\mp$	2.8×10^{-5}	-	$0.97\sqrt{\lambda}$	-	-	$0.62\sqrt{\lambda}$
$B^0 \rightarrow \mu^\pm \tau^\mp$	2.2×10^{-2}	-	$0.18\sqrt{\lambda}$	-	-	$0.12\sqrt{\lambda}$

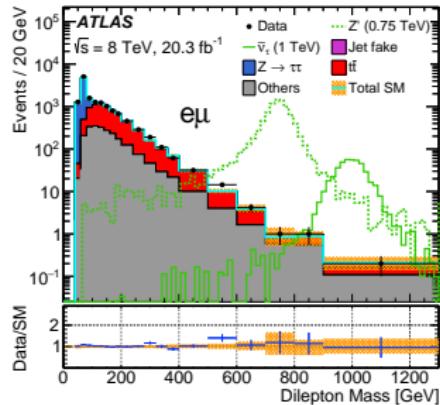
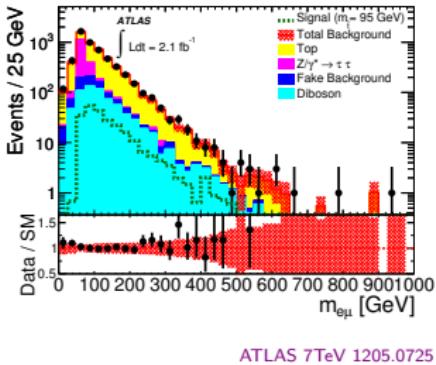
Leptonic Charged Meson Decays $M^+ \rightarrow \ell_i^+ \nu$

- $R_M = \frac{\text{Br}(M^+ \rightarrow e^+ \nu)}{\text{Br}(M^+ \rightarrow \mu^+ \nu)}$
- Theoretical error for R_π (R_K) about 5%
- Improvement by factor 20 (2) possible
- ✓ indicates constraints
- Second index of Λ corresponds to charged lepton



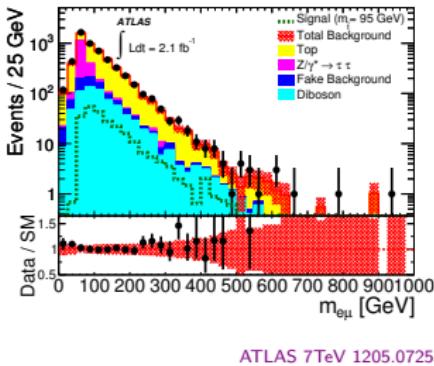
decay	constraint	cutoff scale Λ [TeV]		Wilson coefficients				
		$\Lambda_{\mu e, e\mu, e\tau}$	$\Lambda_{\tau e, \tau\mu, \mu\tau}$	$\Xi_{ij,uu}^u$	$\Xi_{ij,dd}^d$	$\Xi_{ij,ss}^d$	$\Xi_{ij,cc}^u$	$\Xi_{ij,bb}^d$
R_π	$R_\pi^{\text{exp}} \pm 5\%$	25 – 280	25 – 260	✓	✓	-	-	-
R_K	$R_K^{\text{exp}} \pm 5\%$	24 – 160	24 – 150	✓	-	✓	-	-
$\text{Br}(D^+ \rightarrow e^+ \nu)$	$< 8.8 \times 10^{-6}$	2.8 – 2.9	2.9	-	✓	-	✓	-
$\text{Br}(D_s^+ \rightarrow e^+ \nu)$	$< 8.3 \times 10^{-5}$	3.2 – 3.3	3.2 – 3.3	-	-	✓	✓	-
$\text{Br}(B^+ \rightarrow e^+ \nu)$	$< 9.8 \times 10^{-7}$	2.0	2.0	✓	-	-	-	✓
$\text{Br}(\pi^+ \rightarrow \mu^+ \nu)$	$\text{Br}^{\text{exp}} \pm 5\%$	1.9 – 7.4	1.9 – 9.4	✓	✓	-	-	-
$\text{Br}(K^+ \rightarrow \mu^+ \nu)$	$\text{Br}^{\text{exp}} \pm 5\%$	1.7 – 5.8	1.7 – 7.4	✓	-	✓	-	-
$\text{Br}(D^+ \rightarrow \mu^+ \nu)$	$(3.82 \pm 0.33) \times 10^{-4}$	1.1 – 2.7	1.1 – 3.4	-	✓	-	✓	-
$\text{Br}(D_s^+ \rightarrow \mu^+ \nu)$	$(5.56 \pm 0.25) \times 10^{-3}$	1.3 – 4.3	1.3 – 5.3	-	-	✓	✓	-
$\text{Br}(B^+ \rightarrow \mu^+ \nu)$	$< 1.0 \times 10^{-6}$	1.9 – 2.7	1.7 – 3.0	✓	-	-	-	✓
$\text{Br}(D^+ \rightarrow \tau^+ \nu)$	$< 1.2 \times 10^{-3}$	0.21 – 0.78	0.23 – 0.73	-	✓	-	✓	-
$\text{Br}(D_s^+ \rightarrow \tau^+ \nu)$	$(5.54 \pm 0.24) \times 10^{-2}$	0.33 – 1.2	0.33 – 1.1	-	-	✓	✓	-
$\text{Br}(B^+ \rightarrow \tau^+ \nu)$	$(1.14 \pm 0.27) \times 10^{-4}$	0.49 – 1.3	0.49 – 1.2	✓	-	-	-	✓

SM Background

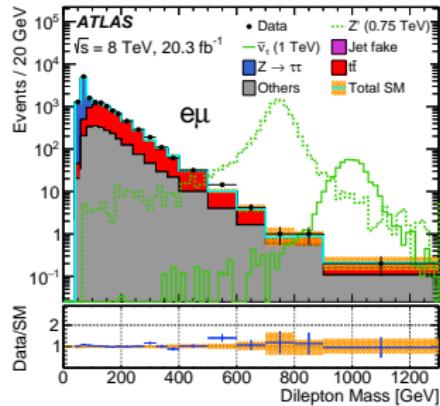


- Main backgrounds: $t\bar{t}$, WW , $Z/\gamma^* \rightarrow \tau\tau$
also W/Z plus jets, WZ/ZZ , single top and $W/Z + \gamma$
- ⇒ Efficiently reduced in exclusive 7 TeV analysis
by rejecting jets and $E_T^{miss} < 20$ GeV
- Modelling of main background agrees with ATLAS
- Fake background estimated from data
- ⇒ Use background from ATLAS publications

SM Background



ATLAS 7TeV 1205.0725



ATLAS 8TeV 1503.04430

- Main backgrounds: $t\bar{t}$, WW , $Z/\gamma^* \rightarrow \tau\tau$
also W/Z plus jets, WZ/ZZ , single top and $W/Z + \gamma$
- ⇒ Efficiently reduced in exclusive 7 TeV analysis
by rejecting jets and $E_T^{miss} < 20$ GeV
- Modelling of main background agrees with ATLAS
- Fake background estimated from data
- ⇒ Use background from ATLAS publications

Selection Criteria

Same selection criteria as in ATLAS 7 and 8 TeV analyses.

- oppositely charged leptons
- Electrons: $E_T > 25 \text{ GeV}$, $|\eta| < 1.37$ or $1.52 < |\eta| < 2.47$, tight identification criteria
- Muons: $p_T > 25 \text{ GeV}$, $|\eta| < 2.4$
- Tau: $E_T > 25 \text{ GeV}$, $0.03 < |\eta| < 2.47$
- Lepton isolation: scalar sum of lepton p_T within cone of $\Delta R = 0.2(0.4)$ is less than 10% (6%) of lepton p_T for 7 (8) TeV search
- Jets reconstructed anti- k_T algorithm with radius parameter 0.4
- 7 TeV analysis: jets rejected if $p_T > 30 \text{ GeV}$ or $E_T^{miss} < 25 \text{ GeV}$
- Invariant mass of lepton pair: $> 100(200) \text{ GeV}$ in 7(8) TeV analysis
- azimuthal angle difference $\Delta\phi > 3(2.7)$ in 7 (8) TeV analysis

14 TeV projection

Same as 7 TeV exclusive analysis and $p_T(\ell) > 300 \text{ GeV}$ and $E_T^{miss} < 20 \text{ GeV}$

Limits from LHC on Cutoff Scale in TeV

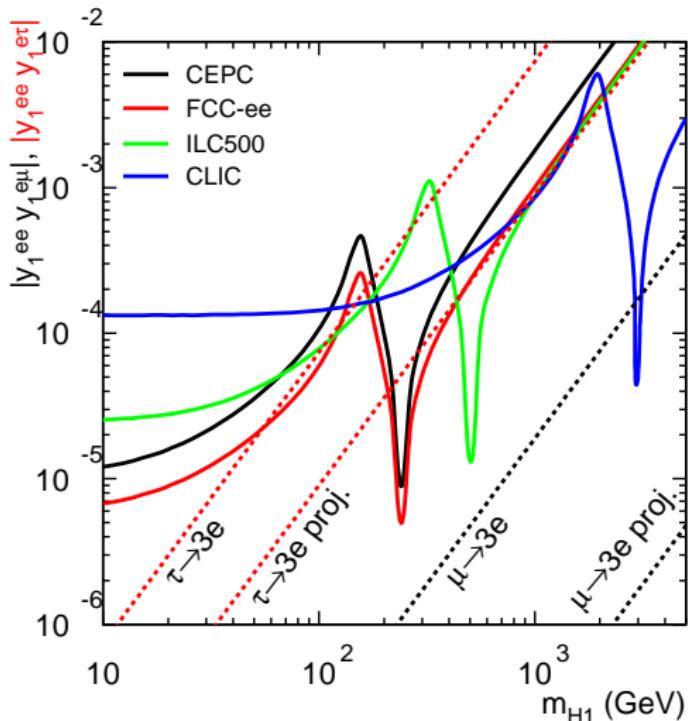
$\bar{q}q$	$\bar{\ell}_i \ell_j$	$\bar{e}\mu$		$\bar{e}\tau$		$\bar{\mu}\tau$
		7 TeV	8 TeV	14 TeV	8 TeV	8 TeV
$\bar{u}u$		2.6	2.9	8.9	2.4	2.2
$\bar{d}d$		2.3	2.3	8.0	2.1	1.9
$\bar{s}s$		1.1	1.4	4.0	0.95	0.88
$\bar{c}c$		0.97	1.3	3.6	0.82	0.78
$\bar{b}b$		0.74	1.0	2.7	0.63	0.61

- 8 TeV analysis gives only a slight improvement compared to 7 TeV despite 10 times more data because of large background
- $e\tau$ and $\mu\tau$ limits weaker than $e\mu$ because of low τ -tagging rate and higher fake background
- 14 TeV projection: same search strategy as 7 TeV exclusive search

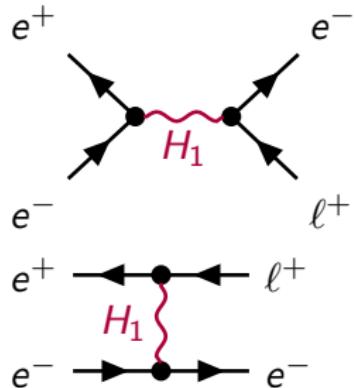
cLFV D8 operator with 2 gluons and 2 leptons

process	exp. limit	operator	Λ [TeV]
$e\mu$			
$\text{Br}(\mu^- \frac{48}{22}\text{Ti} \rightarrow e^- \frac{48}{22}\text{Ti})$	$< 4.3 \times 10^{-12}$	$\mathcal{O}_X, \bar{\mathcal{O}}_X$	2.11
$\text{Br}(\mu^- \frac{197}{79}\text{Au} \rightarrow e^- \frac{197}{79}\text{Au})$	$< 7 \times 10^{-13}$	$\mathcal{O}_X, \bar{\mathcal{O}}_X$	2.54
$e\tau$			
$\text{Br}(\tau^+ \rightarrow e^+ \pi^+ \pi^-)$	$< 2.3 \times 10^{-8}$	$\mathcal{O}_X, \bar{\mathcal{O}}_X$	0.42
$\text{Br}(\tau^- \rightarrow e^- K^+ K^-)$	$< 3.4 \times 10^{-8}$	$\mathcal{O}_X, \bar{\mathcal{O}}_X$	0.37
$\text{Br}(\tau^- \rightarrow e^- \eta)$	$< 9.2 \times 10^{-8}$	$\mathcal{O}'_X, \bar{\mathcal{O}}'_X$	0.40
$\text{Br}(\tau^- \rightarrow e^- \eta')$	$< 1.6 \times 10^{-7}$	$\mathcal{O}'_X, \bar{\mathcal{O}}'_X$	0.44
$\mu\tau$			
$\text{Br}(\tau^- \rightarrow \mu^- \pi^+ \pi^-)$	$< 2.1 \times 10^{-8}$	$\mathcal{O}_X, \bar{\mathcal{O}}_X$	0.43
$\text{Br}(\tau^- \rightarrow \mu^- K^+ K^-)$	$< 4.4 \times 10^{-8}$	$\mathcal{O}_X, \bar{\mathcal{O}}_X$	0.36
$\text{Br}(\tau^- \rightarrow \mu^- \eta)$	$< 6.5 \times 10^{-8}$	$\mathcal{O}'_X, \bar{\mathcal{O}}'_X$	0.42
$\text{Br}(\tau^- \rightarrow \mu^- \eta')$	$< 1.3 \times 10^{-7}$	$\mathcal{O}'_X, \bar{\mathcal{O}}'_X$	0.46

$$H_{1\mu}: e^+e^- \rightarrow e^\pm\mu^\mp(e^\pm\tau^\mp)$$



$$\mathcal{L} = y_1^{ij} H_{1\mu} \bar{\ell}_i \gamma^\mu P_L \ell_j$$

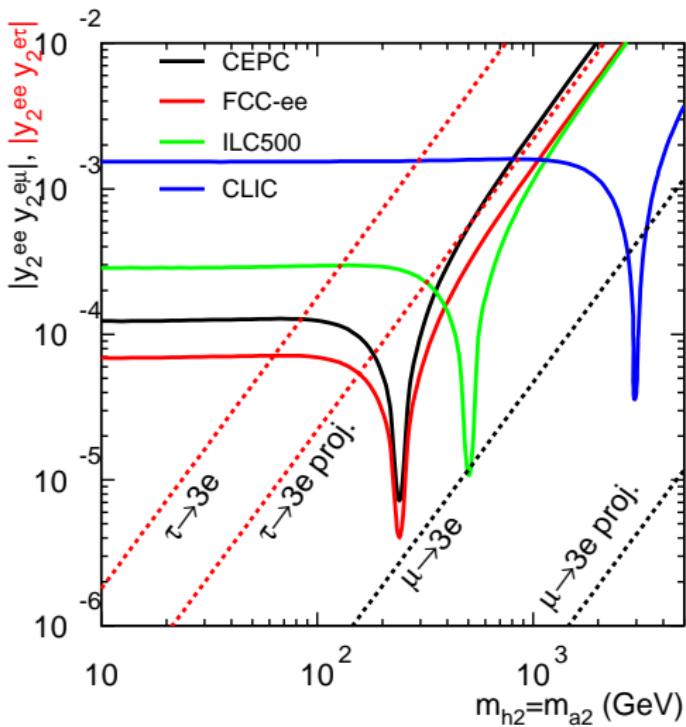


same result for
right-handed $H'_{1\mu}$

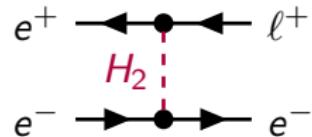
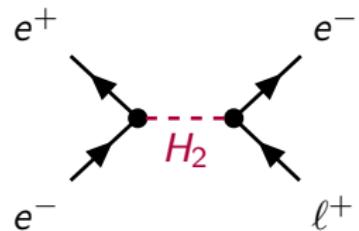
τ efficiency not included in figure

60% τ eff. \Rightarrow 77% (60%) sensitivity reduction for 1 (2) τ leptons

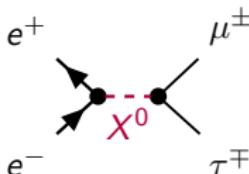
$$H_2: e^+e^- \rightarrow e^\pm\mu^\mp(e^\pm\tau^\mp)$$



$$\mathcal{L} = y_2^{ij} H_2^0 \bar{\ell}_i P_R \ell_j + h.c.$$

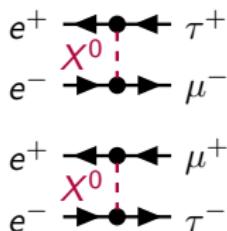
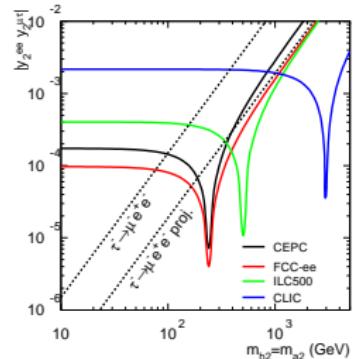
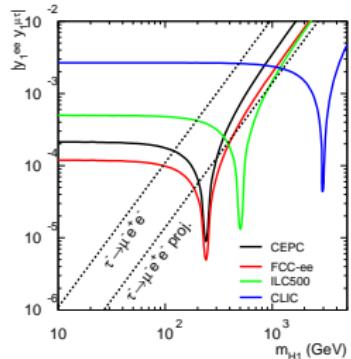


$$H_{1\mu}, H_2: e^+e^- \rightarrow \mu^\pm\tau^\mp$$



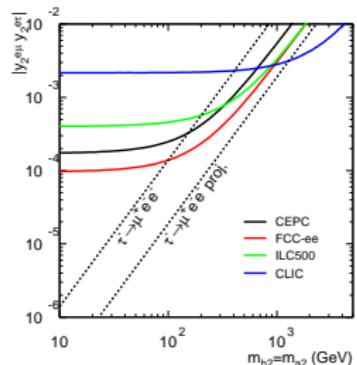
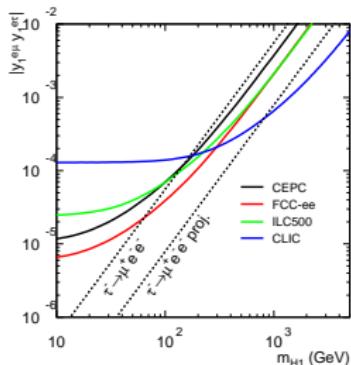
rel. couplings

$$|y^{ee} y^{\mu\tau}|$$

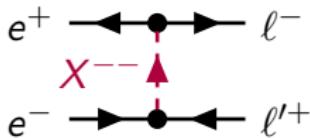


rel. couplings

$$|y^{e\mu} y^{e\tau}|$$

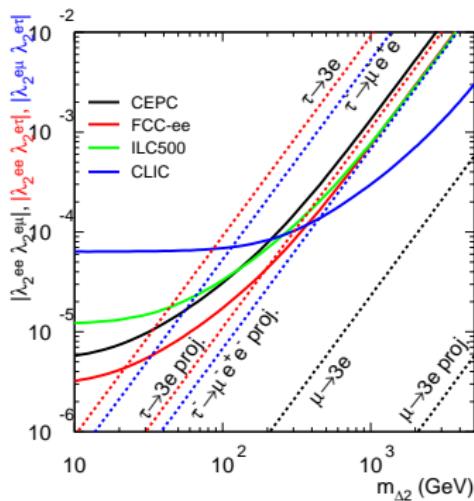
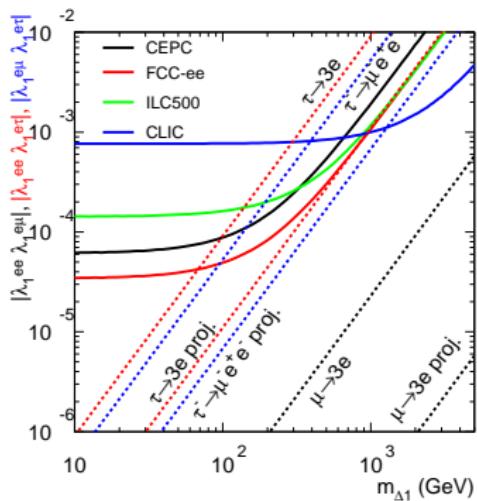


$$\Delta_1, \Delta_{2\mu}: e^+ e^- \rightarrow \ell^+ \ell'^-$$

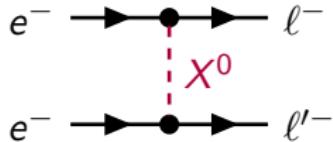


relevant couplings

$$|\lambda^{ee} \lambda^{e\ell}| \text{ and } |\lambda^{e\mu} \lambda^{e\tau}|$$

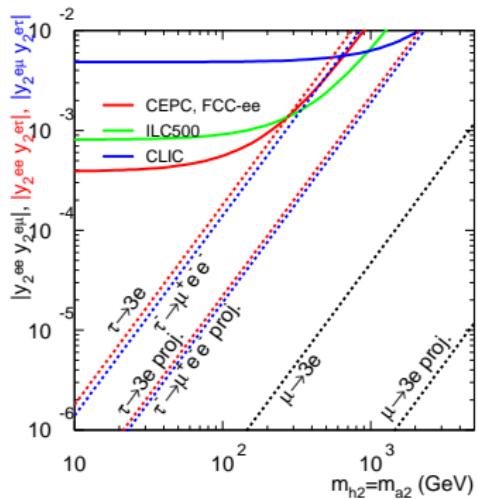
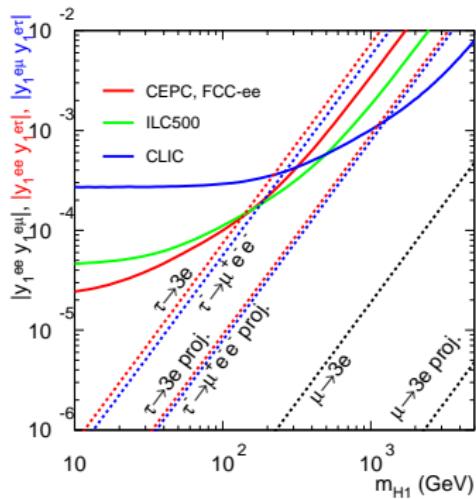


$H_{1\mu}, H_2: e^- e^- \rightarrow \ell^- \ell'^-$

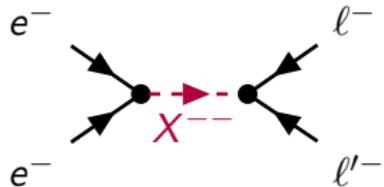


relevant couplings

$|y^{ee} y^{el}|$ and $|y^{e\mu} y^{e\tau}|$



$\Delta_1, \Delta_{2\mu} : e^- e^- \rightarrow \ell^- \ell'^-$



relevant couplings
 $|\lambda^{ee}\lambda^{el}|$ and $|\lambda^{ee}\lambda^{\mu\tau}|$

